Building Embedded Languages and Expert System Shells in Prolog

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Abstract
This paper concerns building embedded languages in Prolog, with special attention on expert system shells. First, the paradigm of meta-programming, of which building embedded languages is an example, is discussed. Second, we review interpreters for embedded languages, concentrating on meta-interpreters. Finally, two applications, explanation and uncertainty reasoning, are presented and the techniques that were used in their construction are discussed.

1 The Paradigm of Meta-Programming

Prolog is widely recognized as a good language for writing simple rule-based expert systems. There are two major factors. First, the primary language constructs, Horn clauses, are essentially rules. Second, Prolog's built-in backward chaining interpreter can be used as the inference engine. However, writing rule-based systems directly in Prolog has limitations due to the 'hardwiring' of both a particular type of representation and a particular inference strategy. Further, the language does not provide certain functionalities of an expert system shell, such as tools for interacting with the user, explanation, knowledge acquisition and debugging.

Three different approaches have been suggested to overcome Prolog's limitations for building expert systems [11]. The first method is to build the desired extensions within the underlying Prolog engine at the implementation level of a Prolog compiler or interpreter. The second method is to translate a knowledge-based system written in a special language to Prolog by using a special compiler. The third method is to exploit the meta-programming facilities of Prolog. Clearly the first method is the most efficient yet the most inflexible. Developing the desired extensions within Prolog is the easiest method and the most flexible one, since it is not necessary to change the underlying Prolog system. In this paper, we advocate this third method and illustrate techniques for building embedded languages and expert system shells in Prolog by exploiting its meta-programming facilities.

Let us start by addressing the question "what is meta-programming", a topic which has concerned many researchers. One common definition [2, 19] states

Meta-programming is writing programs that treat other programs as data.

By this definition, familiar programs, such as assemblers, compilers and program transformers are meta-programs.

Another definition of meta-programming can be obtained by following Hayes-Roth's: Meta-X is a macro definition for 'X about X' [13]. Expanding this macro as in [5], yields another definition of meta-programming.

Meta-programming is programming about programming.

Both of the above definitions are descriptive. However they are missing, in our opinion, the essence of meta-programming by ignoring both the purpose of writing meta-programs and the approach taken for developing them.

We regard meta-programming as a paradigm, which is according to Floyd [12], an approach to writing programs. A paradigm can also be described as a collection of methods and/or techniques to facilitate the construction of certain classes of programs. Other examples of paradigms are structured programming, dynamic programming, divide-and-conquer and object-oriented programming.

We offer a single sentence definition of the paradigm of meta-programming.

Meta-programming is building an abstraction of an object language and developing an interpreter for the abstraction.

This definition does not contradict the previous definitions. However, it focuses on the purpose behind meta-programming activity. The reason for conceiving a programming task as meta-programming is to clarify and simplify the programming by giving a useful language to the user with which to build applications.

In the chapter on meta-linguistic abstractions in their well-known textbook, Abelson and Sussman [1] stress the importance of establishing new descriptive languages for programming. Tools and techniques are needed both to formulate new languages and to implement these languages by constructing evaluators. From an engineering point of view, it is much simpler to build within a high level language by delegating some of the work, i.e. matching, unification, or backward chaining to the underlying system.
Meta-programming is an important paradigm for AI applications. The best way to develop a new application, in our experience, is to design a new language tailored to the application. This is only practical if it is easy to design and implement the language.

A particular language, such as Prolog, supports meta-programming by making it easy to write interpreters for a specific application. Interpreters are used for two related reasons for modeling computations. The first one is the execution of an embedded language within a programming language. The next section gives an example of developing an embedded language within Prolog, and gives a simple interpreter.

The second reason for developing interpreters is to model a particular inference, such as backward chaining. The interpreter can then be used to develop expert system shells. In section 3, we discuss how to develop interpreters, classify the purposes of building them and present relevant techniques. In section 4, we discuss two expert system shells, for uncertainty reasoning and explanation, that exemplify the meta-programming paradigm.

2 Embedded Languages

This section gives an example of designing an embedded language for an expert system application. Before giving the details of the example, it is necessary to define some terminology.

The domain language is the language used to represent knowledge about the problem domain. An object language is a language describing a system or application program. A meta-language is a language which represents the constructs of an object language explicitly. In this paper, we identify the domain and object languages and refer to the two synonymously.

Consider writing an expert system to evaluate graduate student applications to a department in a university. Such a system must weigh attributes of a student such as GRE scores, grades, recommendation letters, and senior project topic, and classify the student applications to a department in a university. The knowledge engineer has the responsibility of modeling the computations. The interpreter can then be used to develop an appropriate interpreter for the language.

The embedded language is more convenient for building expert systems. The knowledge engineer has the possibility of communicating more directly with the expert and reducing the gap between expert knowledge and expert system knowledge. The user does not need to know the full details of Prolog syntax and execution, but can focus on the embedded language.

It is possible to build applications directly in Prolog. A sample rule from our running example follows.

An interpreter is needed to evaluate whether a certain Student satisfies the requirements written in the rule language. Such an interpreter, is given below by the predicate evaluate(Student, Decision). It tries the rules in turn until one is found which is applicable for the given student, essentially using a generate-and-test strategy. By having the representation built on Prolog, two of its features are exploited to evaluate the rules. Firstly, these rules are retrieved by using Prolog's built-in backward chaining interpreter. Secondly, the instantiation of variables is achieved by using Prolog's unification.

evaluate(Student, Decision) ←
Qualifications ← Decision, holds(Qualifications, Student).
holds(C1&V2, Student) ← holds(C1, Student).
holds(C1&V2, Student) ← holds(C2, Student).
holds(C1&V2, Student) ← holds(C1, Student), holds(C2, Student).
holds(Concept, RelOp, ExpVal), Student) ← lookup(Concept, Student, Value), values(Concept, Values), compare(RelOp, ExpVal, Value, Values).

The holds predicate tests that all the Qualifications on the left-hand side of a rule hold with respect to the Student under consideration. It depends on compare/4, which compares the Student's Value with the expected value, ExpVal, of the Concept based on the operator RelOp defined in the rule. Code for compare can be found in [19].

Let us generalize the experience. An embedded language for an application is built by

• identifying the underlying abstraction necessary for the task.
• defining its representation in Prolog by creating language constructs, such as a new representation scheme for rules.
• building an appropriate interpreter for the language.

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A sample rule from our running example follows.

(gre,=,excellent) & (grades,>=,very_good) &
(recommendations,=,very_good) =⇒ accept.
(faculty_decision,=,good) =⇒ accept.
(gre,=,excellent) & (grades,=,good) &
((senior_project,=,interesting) V
(recommendation,=,very_good)) =⇒ consider.
(gre,=,very_good) & (grades,=,excellent) &
(senior_project,=,interesting) &
(recommendation,=,good) =⇒ consider.
(gre,=,excellent) &
(grades,=,bad) =⇒ refuse.
evaluate(Student, accept) ←
    holds((gre, = , excellent), Student),
    holds((grades, >= , very_good), Student),
    holds((recommendation, >= , very_good),
         Student).

Comparing the system implemented directly in Prolog with building a new rule language illustrates the advantages of using an embedded language. This method provides a general framework for other applications which might use the same paradigm. For example, the generate-and-test paradigm for ordinal reasoning was used for two expert system applications, as described in [5]. In addition, flexibility and clarity is achieved by separation of the rules and how they are evaluated. Building on the power of Prolog, it is easier to include new rules or change the inference separately by using an embedded language.

3 Writing Interpreters

In this section, we present a meta-interpreter which makes explicit multiple lines of reasoning. Multiple lines of reasoning are necessary to handle failure and backtracking explicitly. Further constraints we place on our meta-interpreter are that the lines of reasoning are considered in the same order as Prolog.

The meta-interpreter is based on a generate-and-test approach to traverse the AND-OR tree implicitly searched by Prolog. Backtracking is used to search alternative paths upon failure. The meta-interpreter has two layers. The bottom layer performs the computation explicitly, similarly to the well-known vanilla interpreter, with the addition that branches of the search tree are labelled with an auxiliary parameter Result, which takes the values yes for success nodes and no for failure nodes. The computation is monitored by the top layer which generates the computation results and tests them. This abstraction gives the power to represent both success and failure by using a single interpreter. Note that we could not model the computation by using a Result parameter and a bottom layer only, because the goal is to be able to represent multiple lines of reasoning within Prolog. The code for the layered interpreter is given in Figure 1 and is used as a basis for the uncertainty reasoning and explanation shells presented in the next section.

Other techniques are required for meta-interpreters which make different aspects of the computation explicit and available. For example, in order to construct systems for reasoning about belief, or modules,
we need to make theories, i.e., sets of rules, explicit. This is the approach taken in MetaProlog [8]. In order to reason about unification, all aspects of unification such as renaming, matching and propagation of matching in the program clauses have to be explicitly represented. The demo meta-interpreter represents both unification and theories explicitly and is further discussed in [7].

The work presented above is complementary to previous work [17] which advocated using meta-interpreters for expert system construction. There, the emphasis was on systematic ways of adding multiple functionalities to a single meta-interpreter and composing them to get a final interpreter which incorporates the composite functionalities. Composing meta-interpreters was discussed in detail in [18]. Here we emphasize writing different meta-interpreters which are to be used as a basis for describing computations, where the functionalities are added later. How to add and compose functionalities is discussed in [17, 18].

4 Expert system Shells

This section describes two applications based on the paradigm of meta-programming in Prolog, an expert system shell for reasoning under uncertainty and another shell for explanation. Both of these systems exploit the multiple lines of reasoning allowed by the layered meta-interpreter presented in Section 3.

4.1 Uncertainty Reasoning in Prolog Based Expert Systems

Many researchers have addressed methods for incorporating uncertainty reasoning within the paradigm of logic programming [23]. Describing the uncertainty reasoning scheme by using an appropriate Prolog meta-interpreter is the usual approach [15, 19, 16]. However, several issues have not been adequately addressed by previous research. In this section, we show how handling multiple lines of reasoning as allowed by the layered meta-interpreter addresses some of the limitations of previous research. We begin by reviewing the two major concerns for handling uncertainty with Prolog meta-interpreters, namely the representation of uncertainty and the uncertainty reasoning calculus.

Uncertainty is usually represented by augmenting the rule representation with an attached certainty factor. A Prolog clause with augmented certainty factor** indicates a conditional certainty of the head of the clause when the body of the clause is true. For example, in $A \leftarrow cf(CF), B_1, ..., B_n$, the certainty factor $CF$ represents the certainty of $A$ when the body of the clause is true. Clauses without certainty factors are assumed to have the maximum certainty factor 1. The exact form of the certainty factor is not specified, and we discuss both single valued and two valued uncertainties in this section.

The uncertainty calculus describes the methods to evaluate the rules during inference. For example, the best known uncertainty reasoning scheme is used in MYCIN [9], and reasons with single value uncertainties. Dempster-Shafer theory is an example of two valued uncertainty reasoning [4].

The major difficulties with previous work are:

1. Combining Lines of Reasoning: The result of a successful Prolog deduction simply involves one branch in the search tree. There might be, however, other branches in the search tree with the same solution, for a particular answer substitution. It seems sensible to include multiple lines of reasoning when we calculate an uncertainty for a predicate. This is not possible by computing uncertainties considering a single line of reasoning. In [15, 19], uncertainty is computed only by pruning the current branch of the proof tree if necessary. Therefore, different values of uncertainty are given to the same answer substitution corresponding to different branches of the search tree. Given several bodies of evidence as different paths in the search tree, Baldwin [4] addresses computing a composite number in finding a solution for a predicate. There, the separate lines of reasoning are combined by using the computation of the set union of the answers.

Thus multiple lines of reasoning for a predicate are needed to compute a composite uncertainty. The naive approach to get all the lines of reasoning uses a set predicate such as setof as in [16]. However, this approach does not combine the lines of reasoning at different levels of the computation. It is necessary to consider different lines of reasoning for each rule to compute a composite uncertainty and this should be applied to all the rules in the computation.

2. Handling Failure and Negation: Operationally, dealing with negation requires the computation of all lines of reasoning for a goal. The earlier approaches [15, 19], do not deal with negation correctly, since there is no mechanism to incorporate all lines of reasoning. Note that for single valued probabilities, a probability of not $p$ can be obtained after a composite certainty of $p$ is acquired, with the formula $prob$(not $p$) $=$ $1 - prob(p)$.

3. Explicit Representation of True, False and Unknowns: Single valued probabilities do not allow a distinction between false and unknown values. In contrast, a value pair $[\alpha, \beta]$ allows us to represent predicates that are definitely known to be false, by the pair $[0, 0]$, or known to be true by the pair $[1, 1]$. Other methods to represent and calculate with uncertainties by using two values are discussed in [14, 10, 4]. For example, in [4], the interval $[\alpha, \beta]$ also represents the interval of the certainty of the predicate $p$, where $1 - \beta$ is defined to be the support for not $p$ to be true.

One way to handle unknown predicates is to assign them the value $[0, 1]$, indicating the probability can have any value and there is no supporting or refuting evidence. The COOP shell [16] uses a similar convention to [4]. However, unknowns are represented by adding an auxiliary clause in the knowledge base. This method requires updating the knowledge base, in contrast to the meta-interpreter we present which performs all the necessary calculations. The meta-interpreter appropriately enhanced both to compute two valued uncertainties, if there are two deductions for a predicate $p$ with the same answer substitution $\theta$ with the certainties $p_1$ and $p_2$, respectively, then $prob(p) = p_1 + p_2 - p_1 * p_2$.

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**Note that rules augmented with certainty factors are an example of an embedded language.
solve_top(Goal, U, Proof) ←
solve_bottom(Goal, Uncertainty, Proof),
filter_certainty(Uncertainty, Goal, U, Proof).
solve_top(Goal, U, cl(Goal, U, ProofSet)) ←
combine_prob(Goal, U, ProofSet).
solve_bottom(true, T, fact) ← truthval(T), !.
solve_bottom((A, B), and(CA, CB), (PA, PB)) ←
!, % A and B
solve_top(A, CA, PA),
solve_bottom(and(CA, CB, B, PB)).
solve_bottom(not A, invert(CA), not(A, PA)) ←!
, % negation
solve_top(A, CA, PA).
solve_bottom(A, Uncertainty, sys(A)) ←
sys(A), truthval(T), falseval(F), !,
(A ← Uncertainty = T ;
Uncertainty = F).
solve_bottom(A, F, notclause(A)) ←%
% does not exist in the knowledge base...
not clause_new(A, Body, Ci), falseval(F), !.
solve_bottom(A, body(Ci,CBody),
clause(A,Body,ProofB)) ←
clause_new(A, Body, Ci),
solve_top(Body, CBody, ProofB).
solve_bottom(and(C, C, B, PB) ←
not continue_conj(C), !.
% stop calculation !.
solve_bottom_and(C, CB, B, PB) ← continue_conj(C), !,
% if the first conjunct has not failed, continue...
solve_top(B, PB).

filter_certainty(Uncertainty, Goal, U, Proof) ←
continue_conj(C), !,

store_proof(Goal, Proof, U, Proof).

filter_certainty(U, Goal, U, sys(G)) ← !.
filter_certainty(0, Goal, U, Proof) ←
store_proof(Goal, Proof, O), !, fail.
filter_certainty(invert(Cf), Goal, U, Proof) ← !,
U is 1 - Cf.
filter_certainty(and(U1,U2), Goal, U, Proof) ← !,
Uis U1 * U2
filter_certainty(body(CBody,Ci), Goal, U, Proof) ←
U is CBody = Ci,
store_proof(Goal, Proof, U), !, fail.
truthval(1).
falseval(0).

Figure 2: Extended Layered Interpreter for Handling Single Valued Uncertainties

with single valued probabilities and to obtain proof of deduction is given in Figure 2. Due to the layered structure of the interpreter, the status of the computation is available to the top layer. Recall that the traversal of the search tree in the basic layered meta-interpreter is monitored by a Result variable at the top layer. In a computation that involves uncertainties, the meta-interpreter computes an uncertainty rather than a Result, where the uncertainty can be either a single value or a pair of values. The certainty for a particular goal is computed from the certainties of all the branches that led to the solution at the top layer. The bottom layer provides the certainty calculated from a single line of reasoning. The modified filter predicate at the top layer, filter_certainty, continues to compute all different paths that lead to a solution upon success as well as failure in contrast to filter in Figure 1. The predicate store_proof is used to store the branches of the proof temporarily.

When the computation terminates after calculating all lines of reasoning, by the ultimate failure of the first clause of solve_top, the certainty is calculated by the combine_prob predicate. This predicate first groups solutions with respect to different answer substitutions and then combines the certainties for each answer substitution from different lines of reasoning while eliminating the branches that do not support an answer, i.e. branches with 0 probability. It also returns each different solution, in the order it is obtained, consistent with Prolog's behaviour.

The layered interpreter provides several advantages for uncertainty reasoning:

- **Flexibility:** We assign certainty functions at the bottom level and compute them at the top level. This gives us the flexibility to use single valued or interval valued certainties for representing certainties. By modifying filter_certainty and compute_prob different strategies for calculating uncertainty can be obtained using the same architecture. For example, an interval valued uncertainty calculus as outlined in [4, 16] can be used in the same architecture only by changing filter_certainty.

- **Calculation with Unknowns and Negation:** Since the layered interpreter represents failure and hence negation adequately, the calculation of certainties for negated rules poses no problem in our approach. Actually, this is the first meta-interpreter that we know that can handle rules with negation in reasoning with uncertainties. Furthermore, the fail-safe nature of the layered interpreter allows unknowns to be represented by using the meta-interpreter. Unlike [16], no assignment or alteration of the knowledge base is required. This is desirable because the domain independent inference is separated from the representation of the knowledge base.

- **Dependency of Solutions:** Although this is not implemented, the layered approach can be easily extended to check the dependency of the computations for a specific solution. This issue is discussed in [4]. The layered structure can be extended for resolving conflicts at the top layer by examining the lines of reasoning at the bottom layer. Just like the naive representation of multiple lines of reasoning, a non-layered...
architecture is not capable of doing this, because the independence of conflicts with all possible solutions must be checked for each predicate.

4.2 Explanation

An expert system user may require explanation of the system's behaviour, actions, or decisions. Explanation can be introspect, where the user is presented with what is happening in the system and why. An explanation system can also provide a justification of the system's behaviour.

Different users have varying degrees of knowledge about the system and in general need different explanations varying in content and detail. Explanations can be classified according to what type of information they provide in response to users' queries. For example, how and why explanations highlight the reasons behind the system's decisions and computations. When the expert system queries a user to aid in the solution, by supplying additional information, the user might want to know the reasons for the query. A why type of explanation provides the line of reasoning which leads to the system's queries. Other explanations relate to assertions that are made by the user or the system, such as when and by whom certain facts are provided, which of the known parameters have changed. A discussion of classifying user queries and explanations can be found in [21]. Among types of explanations, what-if explanation requires the simulation of another computation by changing certain variables or facts in the system. It does reflect the current or completed behaviour of the system.

An introspective account of a system can only be provided if the system can represent and present its own computations adequately. Meta-interpreters are a flexible and easy means for providing this type of explanation. The required functionality for explanation is to construct a proof structure representing the computations of the domain language. This is achieved by extending an appropriate interpreter by standard techniques. In [19], the vanilla interpreter is extended to give a simple explanation shell.

We suggest the following features from a general purpose explanation shell based on Prolog:

- It should be interactive, posing queries to the user when the information is not in the knowledge base and recording the responses. This demands a dynamic knowledge base.
- It should be able to display reasons for successful, failed and partially completed computations - thereby providing how, why and whynot explanations.
- It should provide alternative solutions when requested.
- User supplied information should be easily obtainable for providing which, when, and what explanations.

Building an explanation shell from single layer interpreters, such as vanilla, suffer from the limitation that success and failure do not mesh well together. Previous research has written separate meta-interpreters for successful and failed computations [8]. This method requires the system to first determine whether a query has succeeded or failed, in order to construct the proof by the appropriate interpreter. However, expert systems are interactive. Users can add knowledge to the knowledge base during the solution of a goal. Using different meta-interpreters to provide explanation for successful and failed queries causes changes to the knowledge base to be lost, or the computation be mis-represented, because a recomputation of the query does not guarantee the currently constructed proof to represent the previous computation correctly. Therefore, we require an integrated interpreter which can compute queries in one pass.

The layered interpreter provides an appropriate basis for an explanation shell. We omit the interpreter for explanation, as its capabilities are discussed in [20] in detail. However, we present specific points which makes this tool desirable.

1. An integrated single interpreter provides the explicit representation of most aspects of Prolog computations by representing the computation in two layers. This feature has two consequences for explanation.

   - The layered interpreter can represent both successful and failed computations in one pass, since it can handle multiple lines of reasoning. This is a very important feature since the proof for both successful and failed queries can be obtained by using the same meta-interpreter. The dynamic changes to the knowledge base does not impose a problem for this framework, and the proof, hence the explanation we obtain from the proof, is faithful to the current computation.

   - Representing computations with negation and the pruning operator cut are no longer a problem by using the correct techniques [22].

2. We expect the expert system shell to provide alternative solutions when requested by the user. The layered interpreter satisfies this constraint.

3. Using Prolog for knowledge representation directly does not provide any information about the assertions to the database. However, using an embedded language provides information about the structure of the knowledge itself. As in our example of Section 2, the special language represents Conditions leading to an Action. If we have the representation available, then the explanations can be extended to incorporate the features of the language. Regarding our example, it is possible to answer queries of the form, What Conditions hold to lead to Action ? What Conditions do not hold to lead to Action ?.

4.3 Conclusions

In this paper, we have characterized meta-programming as a paradigm, and given a definition. Our specific interest is the use of the paradigm for building expert systems in Prolog. We advocate building an embedded language for specific applications, and presented a simple example for ordinal reasoning. An embedded language for a specific task can be designed very easily in Prolog. The advantage is that a user building an application can work with a restricted language instead of having to deal with the full complexities of Prolog. By exploiting the meta-programming capabilities of Prolog, specifying the language constructs, such as special purpose rules or objects, poses no problems. For knowledge engineers, more functionality can be included in the interpreter of the embedded language by separating knowledge representation from in-
ference. Further, a knowledge engineer can modify the system by using both the embedded language and Prolog directly, since they are both directly available.

The other issue addressed is the use of meta-interpreters. Meta-interpreters provide an explicit representation of a particular model of computation. We focussed on a layered interpreter which allows multiple lines of reasoning. The expressive power of the layered interpreter was demonstrated in two applications - a shell for uncertainty reasoning and for explanation.

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