

Angular momentum of $z \sim 1.5$ galaxies and their local analogues with adaptive optics

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ABSTRACT

We present stellar specific angular momentum j_* measurements of two $z \sim 1.5$ galaxies in the KGES sample and 12 DYNAMO $z \sim 0.1$ analogues of high-redshift galaxies. We combine natural seeing integral field spectroscopic data to trace line emission out to high multiples of effective radius r_e , with adaptive optics assisted Keck/OSIRIS observations to trace the rapid rise in rotation curve in the inner regions. Our spaxel-wise integration method gives results that are on average within measurement uncertainty of the traditional rotation curve model method. At $z \sim 0$, combining GMOS and OSIRIS data sets improves the measurement uncertainty in j_* from 13 per cent (GMOS only) or 16 per cent (OSIRIS only) to 10 per cent. At $z \sim 1.5$, systematics allow for at best 20 per cent uncertainty on j_* . DYNAMO analogues of high- z galaxies have low j_* for their stellar mass M_* , and low bulge-to-total light ratio β for their j_*/M_* . The high- z galaxy COSMOS 127977 has j_*/M_* consistent with normal local disc galaxies, while UDS 78317 is consistent with local analogues. However, our high-resolution OSIRIS data reveal that UDS 78317 may be a merging system. We report a relationship between distance to the $\beta-j_*/M_*$ plane and the ratio of velocity dispersion to rotational velocity σ/v_{\max} , where galaxies that deviate more from the plane are more dispersion-dominated due to turbulence. Much of the scatter in M_*-j_* that is not explained by variations in the bulge-to-total ratio or evolution with redshift may be driven by increased turbulence due to star formation, or by treating mergers as rotating discs.

Key words: galaxies: bulges – galaxies: evolution – galaxies: fundamental parameters – galaxies: high-redshift – galaxies: kinematics and dynamics – galaxies: spiral.

1 INTRODUCTION

A galaxy’s angular momentum (AM) J and mass M are two of its fundamental properties, as together they trace the impact of cumulative tidal forces on that galaxy’s size and density evolution (Mo, Mao & White 1998). Stellar AM J_* regulates disc thickness and colour (Hernandez & Cervantes-Sodi 2006) and is a physical proxy for morphology as first shown by Fall (1983) and later Romanowsky & Fall (2012), Obreschkow & Glazebrook (2014),

Cortese et al. (2016), Sweet et al. (2018a), Posti et al. (2018), Fall & Romanowsky (2018, hereafter **RF12**, **OG14**, **C16**, **S18**, **P18**, **FR18**).

It is common to remove the stellar mass scaling of J and instead study stellar specific AM $j_* = J_*/M_*$. The earliest such study was conducted by Fall (1983), who found that $j_* \propto qM_*^\alpha$, with normalization q setting parallel tracks for early- and late-type galaxies, and slope $\alpha \approx 2/3$ in accordance with predictions for cold dark matter (CDM) haloes. **RF12** later analysed the dependence of this relation on bulge-to-total light ratio β , and showed that q differs between disky and bulge-dominated galaxies. Since then, 2D integral field spectroscopic (IFS) studies have confirmed the earlier findings that earlier types with larger bulges have lower j_* ,

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but with important clarifications regarding the slope α , as follows. For a subset of The H I Nearby Galaxy Survey (THINGS; Leroy et al. 2008; Walter et al. 2008) OG14 found that $\alpha \approx 2/3$ for $0 \leq \beta \leq 0.32$, but a 3D fit between M_* , j_* and β yields $\alpha \sim 1$ at constant β . C16, analysing galaxies observed by the Sydney-AAO Multi-object Integral field (SAMI; Croom et al. 2012) Galaxy Survey (Allen et al. 2015; Bryant et al. 2015; Sharp et al. 2015) agreed, finding that $\alpha \gtrsim 2/3$ for single morphology classes and $\alpha \sim 1$ for late types. More recently, S18 showed for THINGS, galaxies in RF12 and a subset of the Calar Alto Legacy Integral Field Area Survey (CALIFA; Sánchez et al. 2012; Husemann et al. 2013; Walcher et al. 2014; Sánchez et al. 2016) that $\alpha = 0.56 \pm 0.06$ for all bulge fractions, and $\alpha = 1.03 \pm 0.11$ for constant β when β is treated as a free parameter. The finding that $\alpha \sim 1$ leads to a tight relation in β - j_*/M_* space, particularly for galaxies that host pseudo-bulges and have bulge-to-total mass ratios smaller than $\beta \lesssim 0.4$. Such galaxies appear to progress along this relation as they build their pseudo-bulges through secular evolution (Wyse, Gilmore & Franx 1997; Kormendy & Kennicutt 2004; Sweet et al. 2018a). Conversely, FR18 did not find separate relations for galaxies that host pseudo-bulges and classical bulges.

At redshifts $z > 1$ galaxies become increasingly disparate from traditional morphological classifications in the Hubble sequence (reviewed in Glazebrook 2013; Madau & Dickinson 2014). The dynamical time of the Universe is shorter, so major and minor mergers are common (Baugh, Cole & Frenk 1996; Weil, Eke & Efstathiou 1998; Tissera 2000). The first stable discs are starting to appear but have clumpy morphologies (Driver et al. 1995; Glazebrook et al. 1995a; Abraham et al. 1996a,b; Conselice, Bershady & Janren 2000; Elmegreen et al. 2005), high gas fractions (Daddi et al. 2010; Tacconi et al. 2013), high rates of star formation (Bell et al. 2005; Juneau et al. 2005; Swinbank et al. 2009; Genzel et al. 2011), and corresponding enhanced turbulence with respect to local spiral galaxies (Förster Schreiber et al. 2009; Wisnioski et al. 2011; Wuyts et al. 2012; Fisher et al. 2014). These high- z galaxies are predicted in the most recent cosmological hydrodynamical simulations to have lower j_*/M_* (e.g. Teklu et al. 2015; Lagos et al. 2018), linked to lower disc stability against formation of their star-forming clumps (Obreschkow et al. 2015). There are few analyses at high redshift, owing to the scarcity of high-resolution observations of such galaxies, and all use the proxy $j = krv$ for some characteristic radius r and velocity v , with proportionality k dependent on the Sérsic index (Sérsic 1963) in an effort to account for the variation in j_* with morphology (Förster Schreiber et al. 2006; Burkert et al. 2016; Contini et al. 2016; Harrison et al. 2017; Swinbank et al. 2017; Alcorn et al. 2018). Most find α consistent with $2/3$, with redshift dependence varying from no evolution (Burkert et al. 2016; Alcorn et al. 2018) up to a factor of $(1+z)^{-1.5}$ (Förster Schreiber et al. 2006).

Samples of nearby galaxies that have properties similar to those at high redshifts are easier to study than their high- z counterparts, given the relative gains in surface brightness and spatial resolution (Glazebrook 2013). The caveat is that local analogues may not be truly representative of high- z galaxies, so it is insightful to compare the two samples where possible. Possible analogues of high- z galaxies include $z \sim 0.1$ DYNAMics of Massive Objects (DYNAMO) sample (Green et al. 2010, 2014) – the turbulent disc galaxies in DYNAMO are analogous to the clumpy discs with high star formation rates found at $1 \lesssim z \lesssim 2$; Lyman-break analogues (LBAs), which are similar to Lyman-break galaxies at $z \sim 3$ in terms of UV luminosity, stellar mass, and star formation rate (Heckman et al. 2005); supercompact LBAs (Basu-Zych et al. 2009; Gonçalves

et al. 2010), with high-velocity dispersions similar to the $z \sim 2$ galaxies of Law et al. (2007); tadpole galaxies (Straughn et al. 2006; Elmegreen & Elmegreen 2010), which each have a single bright star-forming clump with a tail, and appear to be smaller versions of tadpole galaxies at high redshift as first identified by van den Bergh et al. (1996); green peas (Cardamone et al. 2009), which are compact and low mass but have high star formation rates and velocity dispersions, and clumpy morphology. Of these, only DYNAMO has extensive IFS data including an analysis of AM, and then only for four galaxies (Obreschkow et al. 2015).

Whether locally or at high redshift, j_* is difficult to measure. The best practise is to integrate over spatially resolved J_i in spaxels i from resolved velocity and mass maps, as in OG14, C16, and S18. OG14 demonstrated that using 2D IFS affords an order-of-magnitude improvement in precision over integrated or long-slit spectroscopic observations of local galaxies. Ideally, one aims to reach large multiples of the effective radius r_e in order to trace the bulk of j_* , e.g. $0.99j_*$ is enclosed within $3r_e$ (Sweet et al. 2018a). To do so requires sufficient signal to noise at the faint outskirts of the galaxy. One also desires to adequately sample the inner regions of the galaxies where the rotation curve is rapidly rising, in order to sufficiently constrain the velocity field. This requires adaptive optics (AO)-assisted IFS observations, but the improved PSF and finer sampling come at the price of signal to noise, so such data are less suitable for probing to large multiples of r_e , as discussed in Glazebrook (2013). [One exception may be the recent deep AO imaging for the SINS/zC-SINF survey at $z \sim 2$ (Förster Schreiber et al. 2018), but AM measurements have not yet been presented.] The combination of seeing-limited and AO-assisted IFS data to measure j_* was first demonstrated by Obreschkow et al. (2015, hereafter O15) for four galaxies in DYNAMO. O15 found that their j_* is three times lower for their M_* than normal local galaxies. These analogues have $\beta < 0.1$ so their low j_* is not a consequence of their photometric morphology but may be related to their star formation-induced turbulence.

In this work, we combine natural seeing data to trace low surface brightness outskirts of the galaxies and the bulk of j_* , with AO-assisted data to mitigate the effects of beam-smearing in the high surface brightness inner regions, giving improved constraints on the velocity field. We present the first such measurement for galaxies at high redshift ($z \sim 1.5$) along with measurements for 12 local analogues from the DYNAMO sample.

In Section 2, we describe the samples and our data sets. Section 3 contains the details of our methods for making the measurements presented in this paper. In Section 4, we analyse the relative merits of seeing-limited and AO-assisted data, and the combination of the two. We analyse the relation between stellar mass, specific AM and morphology for high- z galaxies and their local analogues in Section 5. Section 6 discusses possible future evolution of DYNAMO galaxies and the implications in light of our $z \sim 1.5$ observations. Section 7 concludes the paper.

We assume a cosmology where $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_M = 0.27$, and $\Omega_\Lambda = 0.73$, and quote comoving coordinates.

2 SAMPLE AND OBSERVATIONS

We compare the AM properties of two galaxies at $z \sim 1.5$ with 12 local turbulent galaxies in DYNAMO, which have been suggested as local analogues of high- z galaxies, and normal local galaxies from THINGS, RF12, and CALIFA that were presented in S18. The sample selection, observations, and data processing for the DYNAMO and $z \sim 1.5$ samples are described in this section.

2.1 DYNAMO – low-redshift analogue sample

The DYNAMO sample (Green et al. 2010, 2014) is a set of 95 star-forming galaxies at $z \sim 0.1$ selected from the Sloan Digital Sky Survey Data Release 4 (Adelman-McCarthy et al. 2006) as having high $H\alpha$ fluxes due to star formation $L_{H\alpha} > 10^{42}$ erg s $^{-1}$. DYNAMO galaxies are analogous to rotating disc galaxies at $1 \lesssim z \lesssim 2$ in that they have similarly high-velocity dispersions (Green et al. 2010; Bassett et al. 2014) and clumpy morphologies (Fisher et al. 2017b). Their specific star formation rates match those of galaxies between $0 \lesssim z \lesssim 2$ (Green et al. 2010, 2014; Fisher et al. 2019).

For this and related projects we observed a subset of 20 DYNAMO galaxies. Seeing-limited observations were obtained with Gemini GMOS (Hook et al. 2004) for 13 of the 20, and emission line intensity and velocity maps measured at $H\beta$ 4861 Å (Fisher et al. 2017a). Keck OSIRIS (Larkin et al. 2006a,b) AO observations covering the $P\alpha$ 18750 Å line were obtained for another 13 of the sample (Oliva-Altamirano et al. 2018); 7 have both GMOS and OSIRIS data.

Fisher et al. (2017b) presented *Hubble Space Telescope* (*HST*) narrow-band $H\alpha$ and continuum imaging for 10 of the galaxies, using the FR647M, FR716N, and FR782N ramp filters on the Wide Field Camera/Advanced Camera for Surveys (ACS). This imaging is used to constrain inclination and scale length, and for surface density images, for which we assume a constant mass-to-light ratio.¹ We use medium-band imaging for the galaxies that have those data, and narrow-band otherwise. OSIRIS 1.9 μm maps are used for the galaxies that do not have any *HST* imaging.

2.2 KGES – high-redshift sample

Our high-redshift sample is drawn from the KMOS Galaxy Evolution Survey (KGES; Tiley et al. in preparation). KGES comprises KMOS (Sharples et al. 2013) observations of $H\alpha$, [N II]6548 and [N II]6583 emission from 285 galaxies at $1.3 \lesssim z \lesssim 1.5$ in well-known extragalactic fields (COSMOS, CDFS, and UDS). Target galaxies were predominantly selected to be bright ($K > 22.7$) and blue ($I - J < 1.7$), with higher priority assigned to those that have an established spectroscopic redshift. The KMOS PSF FWHM for the targets in this work is 0.6.

We observed two KGES targets, COSMOS 127977 and UDS 78317, with Keck OSIRIS during 2017 December 5–7 in the Hn4 and Hn3 filters, respectively, in order to cover rest-frame $H\alpha$ 6563 Å. These data were processed using the current OSIRIS data reduction pipeline DRP 4.0.0 using rectification matrices taken on 2017 December 14–15. Emission line intensity and velocity maps were then extracted from the data cubes. The OSIRIS PSF FWHM for these observations is 0.1.

Surface density maps are derived from *HST* ACS *I*-band *F814W* archival imaging assuming a constant mass-to-light ratio, with COSMOS 127977 imaging from the Cosmic Evolution Survey (COSMOS; Scoville et al. 2007) (*HST* program 9822), and UDS 78317 imaging from the Cosmic Assembly Near-IR Deep Extragalactic Legacy Survey (CANDELS; Koekemoer et al. 2011) (*HST* program 12064).

Maps of COSMOS 127977 and UDS 78317 are shown in Figs 1 and 2, illustrating that the seeing-limited data probe to higher

radii, while the AO-assisted data are more sensitive to structure, particularly in the inner regions of the galaxy.

3 METHODS

3.1 Specific angular momentum

For each galaxy we combine two data sets to calculate j_* from spatially resolved IFS observations, using the methods of OG14, O15, and S18. The two complementary data sets are (a) AO-assisted OSIRIS observations, which are sensitive to the rapidly changing inner regions of the rotation curve, minimizing the effects of beam smearing and (b) seeing-limited GMOS/KMOS data, which are more sensitive than OSIRIS to the low surface brightness outer regions where the rotation curve becomes flat, in an effort to trace the bulk of the AM. In the spaxels where both data sets have $S/N < 3$ we include a model estimate to extrapolate the surface brightness and velocity profiles to $r_i = \infty$.

Below we describe the steps taken in our calculation:

(1) The observed deprojected spaxel-wise AM J_i is derived separately for the AO-assisted and the seeing-limited kinematic data, where the calculation $J_i = r_i v_i m_i$ is performed in every spaxel i at deprojected radius r whose circular velocity v is derived from ionized gas kinematic maps² and mass m from stellar surface density maps derived from the *HST* images described in the previous section, assuming a constant mass-to-light ratio. The kinematic centre is computed by minimizing the convolution of the light-weighted velocity field with its 180 deg rotation. Inclination and position angle are assumed to be constant with radius and are derived from a fit to the *HST* imaging. We do not treat non-circular motions in this paper; in a future paper we will investigate the contribution of non-circular motions to total j_* and spatially resolved PDF(j_*).

(2) The model J_i in every spaxel is also computed by fitting an exponential profile $\tilde{v}_i \approx v_{\text{flat}}(1 - \exp(-r_i/r_{\text{flat}}))$ to the velocity field, where r_{flat} is the radius at which the velocity reaches the converged velocity v_{flat} . The surface mass density is estimated by fitting $\tilde{\Sigma}(r_i) \approx s_d \exp(-r_i/r_d)$ to the imaging, where s_d is the fitted surface mass density normalization and r_d is the exponential disc scale length. The resulting model is then

$$\tilde{J}_i = r_i \tilde{v}_i \tilde{\Sigma}(r_i) = r_i v_{\text{flat}}(1 - \exp(-r_i/r_{\text{flat}}))s_d \exp(-r_i/r_d). \quad (1)$$

The fitted rotation curves used to derive the model are shown in Fig. 3. On average, the model is consistent with the observed J_* to the 5 per cent level, when integrating over the same high signal-to-noise spaxels. We reiterate that the model simply serves as an estimate of J_i in the low signal-to-noise spaxels and allows to reach the total AM.

(3) The total j_* is then given by combining (1) and (2) to calculate J_*/M_* , where $J_* = |\sum^i J_i|$ is the norm of the sum over

(a) the observed J_i from AO-assisted data in the spaxels where the AO-assisted data have $S/N > 3$,

²We assume that the ionized gas corotates with the stars, expecting that the asymmetric drift between the two is negligible due to their comparable velocity dispersions (Bassett et al. 2014). At high redshift the validity of this assumption is an open question. El-Badry et al. (2018) found that the assumption of corotation tends to cause j_* to be overestimated by around 20 per cent for galaxy disc components. If the assumption of corotation is invalid for our bulgeless $z \sim 1.5$ sample galaxies to a similar extent as it is for FIRE galaxies, then j_* would similarly be reduced by 0.1 dex and the main conclusions of the paper would be unchanged.

¹As we are concerned with *specific* AM, the mass normalization cancels in our calculations.

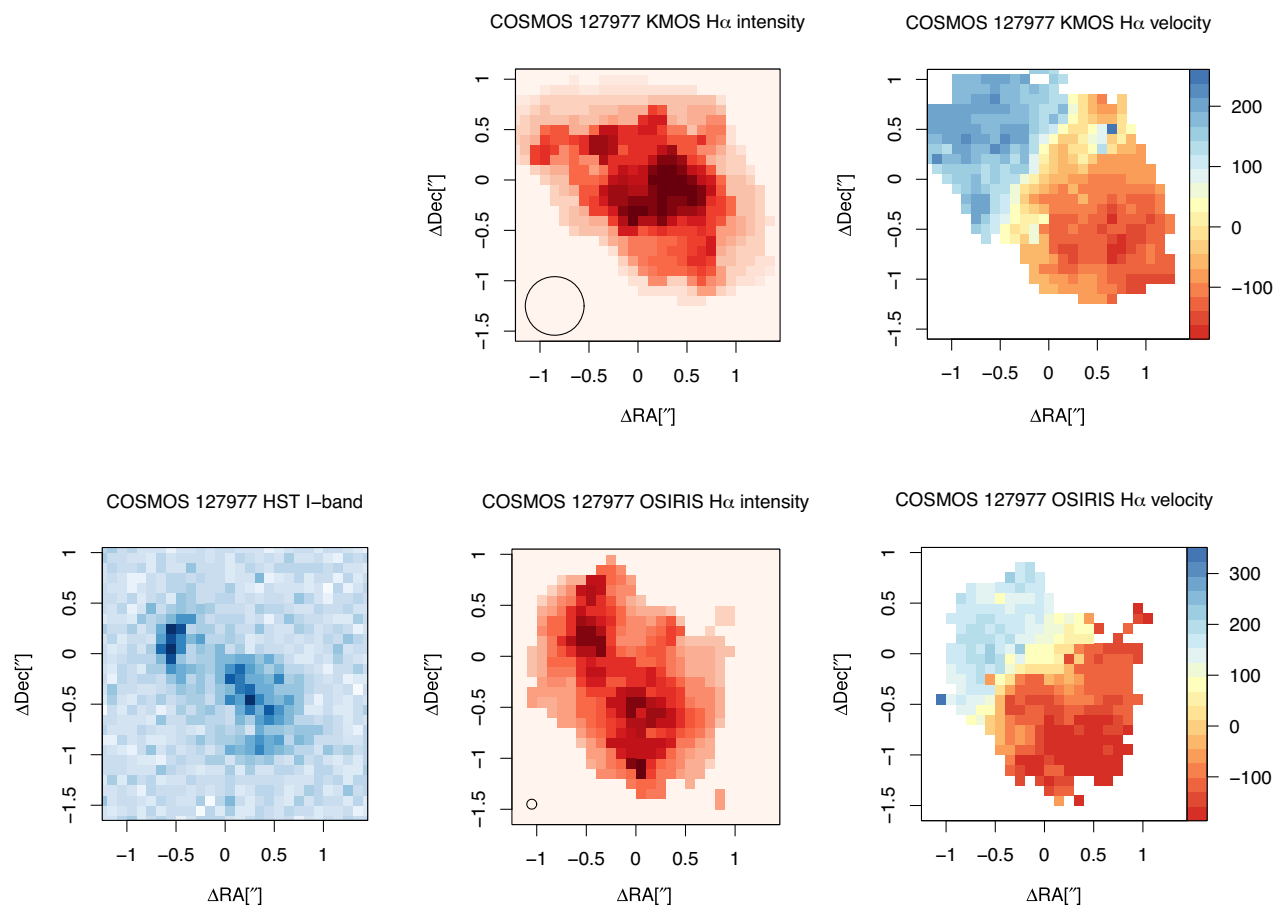


Figure 1. Ionized gas and continuum maps of COSMOS 127977 at $z = 1.62$. Top row: KMOS $H\alpha$ intensity, $H\alpha$ velocity. Bottom row: *HST* I -band continuum, downsampled to 0.1×0.1 arcmin spaxels, OSIRIS $H\alpha$ intensity, OSIRIS $H\alpha$ velocity. The circle in the centre panels denotes PSF FWHM. The natural seeing maps probe higher radii, while the AO-assisted maps detect more structure due to the finer PSF.

(b) the observed J_i from seeing-limited data in the spaxels where the seeing-limited data have $S/N > 3$ and AO $S/N < 3$, and,

(c) the estimated J_i in other spaxels, integrated to $r_i = \infty$.

In this way, the AO data contribute in the inner regions, the seeing-limited data contribute in the outer regions where the AO data are missing or lack the sensitivity to be reliable, and the model contributes elsewhere. The natural seeing v_i measurements are only used in the outer regions where dv/dr is small, so the effect of beam-smearing is also small. Including the estimated J_i in the spaxels where data are missing comprises an average of 13 per cent of the total j_* . In Figs 4 and 5, we show the cumulative stellar specific AM as a function of radius in order to illustrate the contribution to j_* by the AO-assisted data, the natural seeing data, and the model-informed estimate.

This method differs from traditional measurements in the following ways:

(i) Long-slit spectroscopy, such as in RF12, can suffer from misalignment between the kinematic and photometric major axes. The 2D nature of IFS means that the kinematic major axis need not be known *a priori* (Sweet et al. 2016).

(ii) Most other work, whether long-slit or IFS, utilizes the proxy $\tilde{j}_* = kr v$, with single fitted characteristic radius r and velocity v , and the factor $k = k(n)$ an empirical function of Sérsic index n in an effort to account for the variation in j_* with morphology.

However, the velocity fields of many galaxies may not always be well described by simple 1D rotation curves assumed by this model. OG14 showed for nearby spiral galaxies that spaxel-wise integration of fine spatial resolution IFS data gives an order-of-magnitude improvement in *precision*.³ The corresponding correction is described by

$$\left(\frac{j_*}{10^3 \text{ kpc km s}^{-1}} \right) \approx 1.01 \left(\frac{\tilde{j}_*}{10^3 \text{ kpc km s}^{-1}} \right)^{1.3}. \quad (2)$$

This is likely to be even more critical for high- z and local clumpy galaxies, such as those presented in this work. In this work, we compare the spaxel-wise integration method to the traditional rotation curve model method for local turbulent DYNAMO disc galaxies as well as two $z \sim 1.5$ systems.

(iii) In the inner regions of the galaxy, where the rotation curve is rapidly changing, beam smearing can cause the velocity field to be underestimated. This is particularly an issue for seeing-limited observations of high- z objects, and can be ameliorated by AO-assisted data of sufficient quality.

³We note that at high redshifts, where physical spatial resolution is coarser, the decrease in uncertainty may not be so dramatic. However, we choose to use this consistent method throughout the paper.

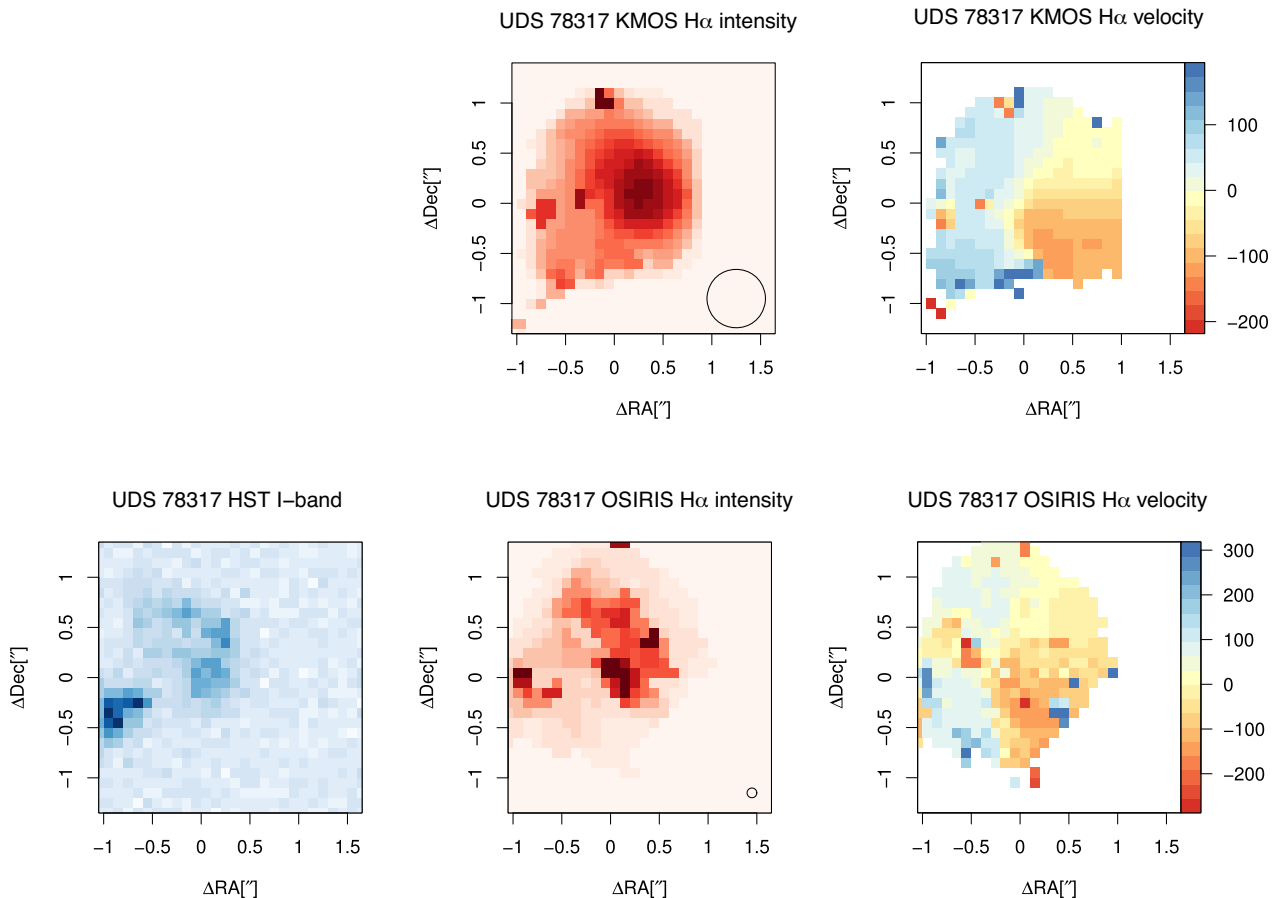


Figure 2. As for Fig. 1 but for UDS 78317 at $z = 1.47$.

(iv) Reaching the outskirts of the galaxy is critical to trace the bulk of the AM (e.g. $0.99j_*$ at $3r_e$, as in Sweet et al. 2018a). AO-only data often lacks the sensitivity to reach such high multiples of the effective radius, so we mitigate this by including seeing-limited data as well.

We demonstrate (ii), (iii), and (iv) in this paper.

The method described above was performed on the two $z \sim 1.5$ galaxies and 20 DYNAMO galaxies described in the previous section. We discarded eight DYNAMO galaxies where the fit failed due to poor S/N or disturbed kinematics indicative of a merger, in order to obtain a meaningful control sample against which to compare the $z \sim 1.5$ galaxies. Six of the remaining 12 galaxies were observed with both AO and natural seeing, and our measurements for those are presented in Table 1. We take the philosophy that (modulo S/N) more data generally gives a truer result, and adopt the combined seeing-limited and AO measurements in preference over the seeing-limited or AO data alone. The exceptions are C22-2, where the AO data are too shallow and limited in radial extent to give any improvement over the seeing-limited observations, and SDSS 013527-1039, where the sky is poorly constrained in the natural seeing map. The final adopted results for the 12 DYNAMO and two $z \sim 1.5$ systems are presented in Table 2. Note that four of these DYNAMO galaxies (C22-2, D13-5, G04-1, G20-2) were presented in O15. Since that paper, we have obtained additional observations, and improved our analysis software to better exclude low S/N spaxels and more carefully fix the kinematic centre, inclination,

and position angle. The j_* values in this work consequently differ from those in O15; they are within errors on average, but individual galaxies differ by between 28 and 69 per cent. Relative uncertainties have decreased from 13.5 per cent to 10 per cent.

3.2 Bulge-to-total ratios

We measure bulge-to-total mass ratios β for the DYNAMO galaxies using *HST* imaging where available, and IFS continuum maps otherwise, using the methods described in Savorgnan & Graham (2016). Briefly, multiple components including bulge, disc, AGN, bar, and ring are identified from the images and unsharp masks. Corresponding Sérsic, exponential, Gaussian, Moffat, Ferrer, and symmetric Gaussian ring components are simultaneously fit to the circularized 1D light profile, where the final functional forms are chosen through an iterative process in order to minimize the residuals.

For the high- z galaxies we use the *HST* archival imaging to estimate β using a similar method to the 2D bulge-disc decompositions described in Fisher & Drory (2008) and used for the THINGS galaxies that are presented in S18 and included in this work. In both cases, the photometry is consistent with a bulgeless galaxy.

The two methods both include a careful, iterative approach and are not reproducible with automatic routines (Fisher & Drory 2008; Savorgnan & Graham 2016). Despite the differences they have been shown to achieve consistent results for the same galaxies, with the 1D fits undertaken for DYNAMO because of the lower failure

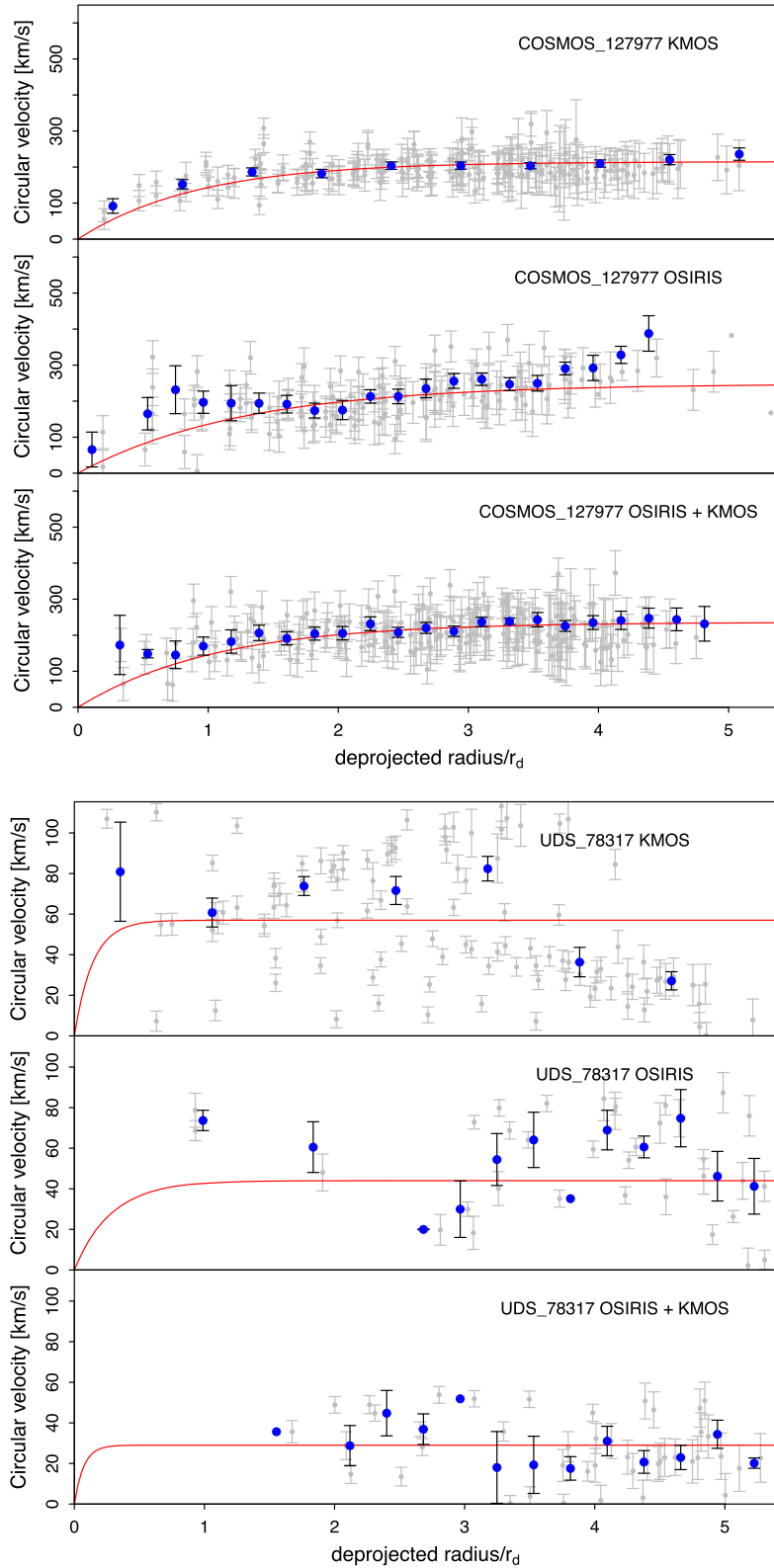


Figure 3. Rotation curves for natural seeing (top panel), AO-assisted (middle panel), and natural seeing and AO combined data (bottom panel). Grey points are the unbinned spaxels (after a sigma-clip for clarity only), blue points are binned spaxels, red curve is the model fit used to extrapolate when calculating total j_* . Top: COSMOS 127977. The natural seeing data are more sensitive to the low surface brightness outer regions of the galaxies, while the AO-assisted data are less affected by beam smearing, particularly in the inner parts where the rotation curves are rapidly rising. The combination of the two data sets allows for better characterization of total stellar specific $AM_{j_{\text{tot}}}$. Bottom: UDS 78317. This galaxy is not well fit by the model rotation curve since it is not a regular disc but a merger, as revealed by the AO maps shown in Fig. 2.

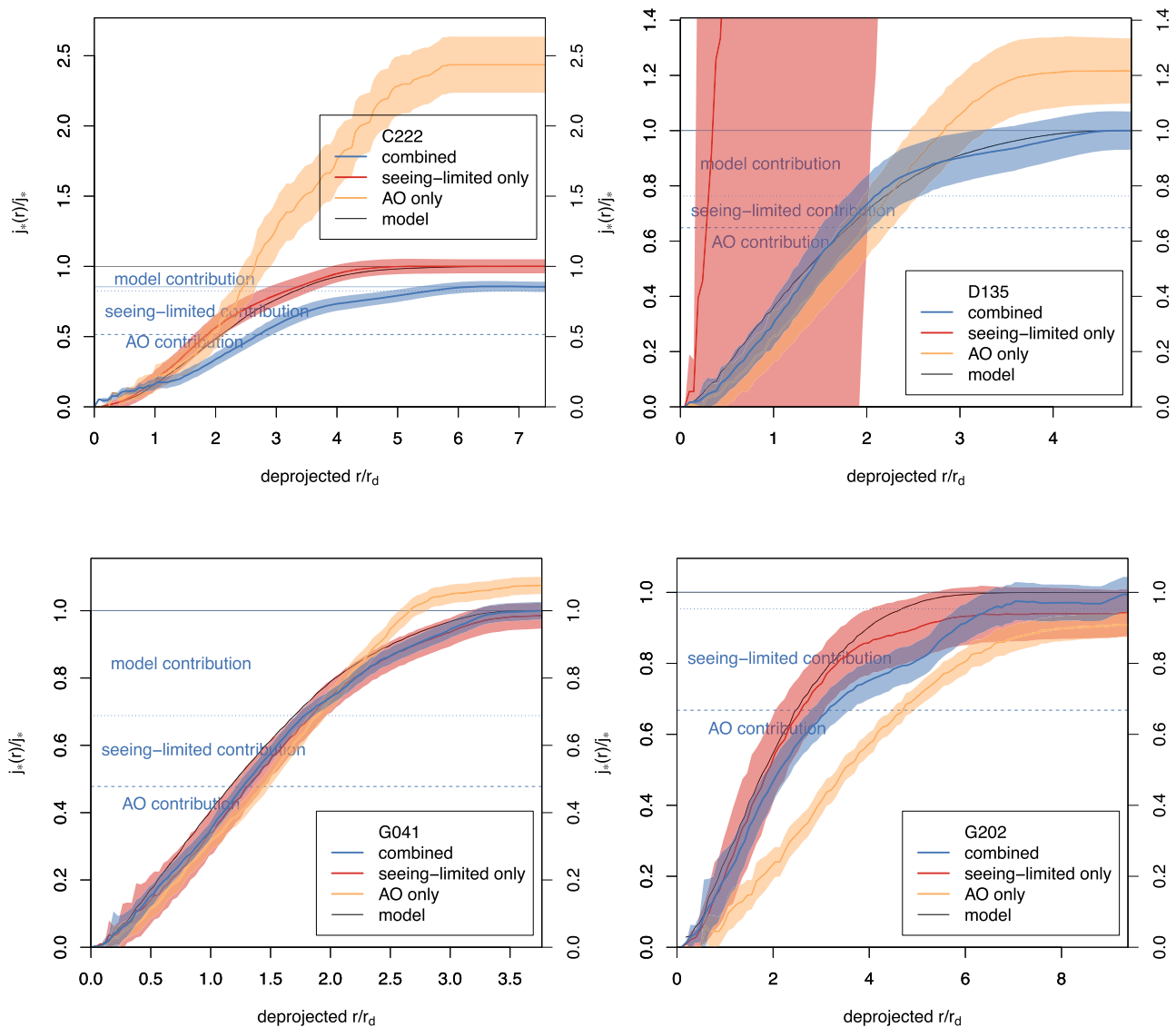


Figure 4. Cumulative specific AM as a function of radius. The blue profile represents the combined data set, with labels showing the contribution from AO-assisted data, seeing-limited data, and model-informed estimate. The orange and red profiles indicate the same measurement made solely with seeing-limited or AO-assisted data, respectively. The transparent shading indicates the uncertainty on each cumulative profile. The black line gives the model profile. The y-axis is normalized to the adopted j_* measurement as given in Table 2. The horizontal lines represent the relative contribution of each component to the combined (blue) profile; due to our spaxel-wise integration method, which accounts for azimuthal variation in S/N of the various data sets, these are simply an approximate mean boundary rather than a strict radial cut. Only the galaxies with both natural seeing and AO data are shown in this figure. Section 4 has more details.

rate for decompositions and more instructive isophotal analysis (Savorgnan & Graham 2016). The 2D fits were appropriate for the more distant $z \sim 1.5$ sources with lower physical resolution.

3.3 Stellar masses

Our integrated stellar mass measurements for the DYNAMO sample are derived from 2MASS K_s -band apparent magnitudes ($4R_s$, i.e. 99 percent of the light), with Galactic extinction correction according to Schlafly & Finkbeiner (2011). We conduct an empirical k -correction (Glazebrook et al. 1995b) with a universal mass-to-light ratio $M/L_{K_s} = 0.5 M_\odot/L_\odot$ assuming a Kroupa (2001) IMF for consistency with the THINGS, RF12, and CALIFA samples

from S18, which we include here as control samples. The typical error introduced by assuming a constant M/L ratio is less than 20 percent (Bell et al. 2003). Using stellar masses following the methods in Kauffmann et al. (2003) instead does not change the results of this paper, but not all of the DYNAMO samples have these available so we opt for the more complete set of measurements.

The $z \sim 1.5$ masses are derived from SED fitting with HYPER-Z (Bolzonella, Miralles & Pelló 2000), using the methods described in Swinbank et al. (2017). We adopt measurement uncertainties of a standard 0.2 dex to conservatively account for deviations in results between common SED fitting codes, and possible effects of low photometric signal to noise (Mobasher et al. 2015).

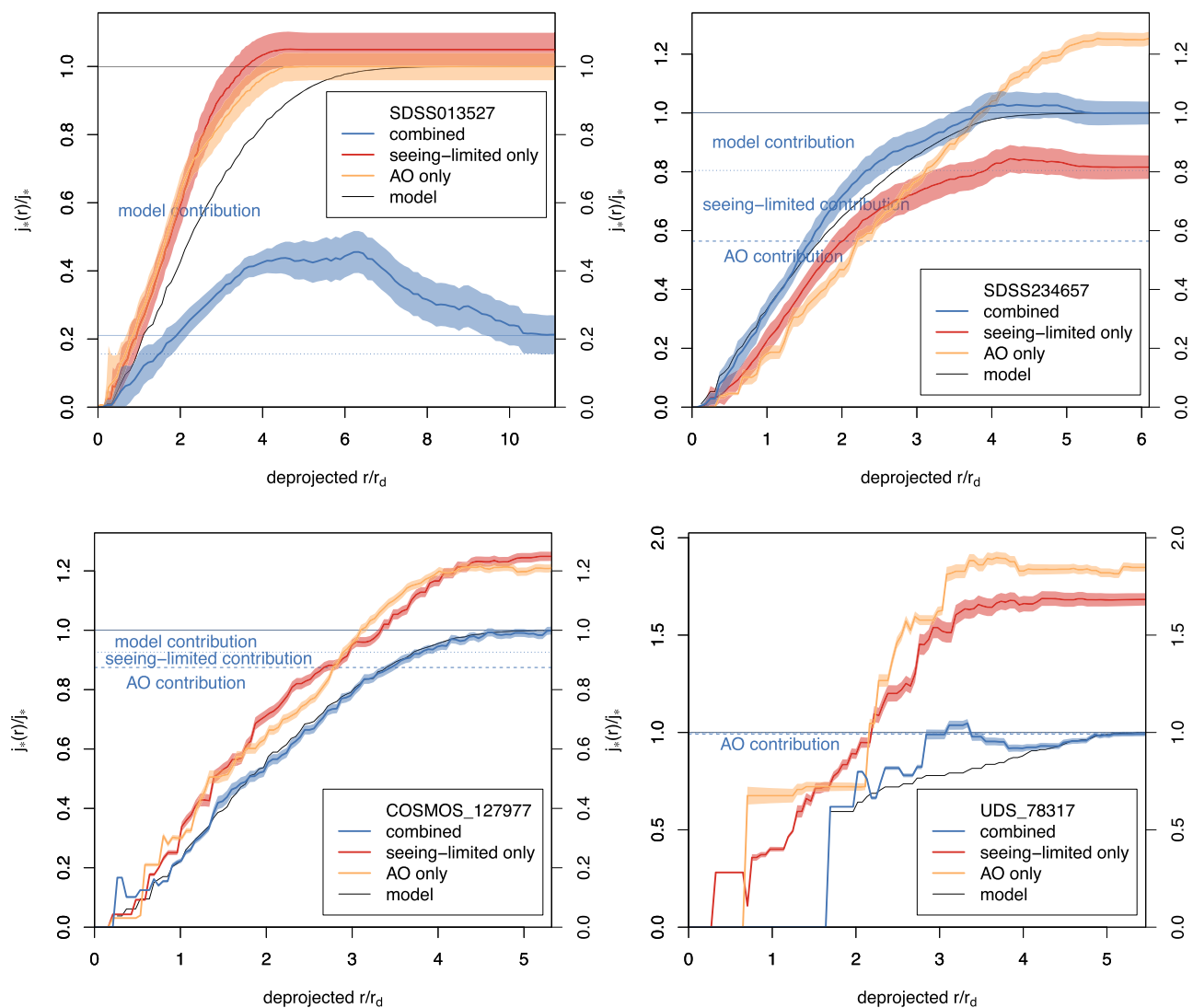


Figure 5. (Continued from Fig. 4) Cumulative specific AM as a function of radius, showing the contribution from AO data, seeing-limited data, and model-informed estimate. Only the galaxies with both natural seeing and AO data are shown in this figure.

3.4 Velocity dispersions

In the $z \sim 1.5$ galaxies, the velocity dispersions are calculated as the median of the KMOS observed dispersion map, corrected for instrumental broadening and beam smearing according to the methods of Johnson et al. (2018). Briefly, we create KMOS data cubes for 10^5 model galaxies and convolve these intrinsic data with PSFs typical of the sample to obtain mock observed data. We compare the properties of the intrinsic and mock observed cubes to obtain correction factors that can be applied to the sample.

For DYNAMO, the velocity dispersions are assumed to be constant across the disc and are derived from fits to the GMOS observations, as described in Fisher et al. (2019).

Velocity dispersions for THINGS are based on CO measurements presented in Mogotsi et al. (2016), under the assumption that CO dispersions trace $H\alpha$ dispersions, as discussed in White et al. (2017) for gas-rich, turbulent DYNAMO galaxies, and demonstrated for one disc galaxy at $z = 1.4$ by Übler et al. (2018).

4 THE EFFECT OF IMAGE QUALITY ON MEASURED SPECIFIC ANGULAR MOMENTUM

In this section, we discuss the effects of spatial resolution and radial coverage on the determination of AM. We present the 2D maps and 1D rotation curves for the two $z \sim 1.5$ systems, and then give a quantitative comparison of specific AM measured in the three data types (seeing-limited, AO, combined) as described in Section 3, for the $z \sim 1.5$ COSMOS 129799 galaxy as well as for local turbulent galaxies in the DYNAMO sample.

Figs 1 and 2 show resolved maps of $H\alpha$ intensity and velocity for natural seeing KMOS observations and OSIRIS AO-assisted data. For both COSMOS 127977 and UDS 78317, the seeing-limited maps probe to larger radii than the AO maps, while the AO maps display more structure. For COSMOS 127977, the AO $H\alpha$ intensity map confirms the clumpy nature of this galaxy seen in *HST* imaging. The difference in substructure between AO and seeing-limited maps is at the scale of the KMOS PSF and can

Table 1. Measured properties of DYNAMO and $z = 1.5$ galaxies for natural seeing, AO and combination of natural seeing and AO.

Name	Obs	z	r_{flat} (kpc)	v_{flat} (km s ⁻¹)	j_* (kpc km s ⁻¹)	Δj_* (kpc km s ⁻¹)	\tilde{j}_* (kpc km s ⁻¹)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
C22-2	GMOS	0.071	1.3	164	449	53	498
C22-2	OSIRIS	0.071	2.5	247	1101	216	1281
C22-2	GMOS + OSIRIS	0.071	2.5	171	384	39	413
D13-5	GMOS	0.075	0.5	182	10 343	2068	10 342
D13-5	OSIRIS	0.075	0.4	174	567	88	565
D13-5	GMOS + OSIRIS	0.075	0.4	171	466	51	437
G04-1	GMOS	0.130	1.5	227	976	124	1051
G04-1	OSIRIS	0.130	0.9	242	1065	173	1119
G04-1	GMOS + OSIRIS	0.130	0.7	221	991	118	1025
G20-2	GMOS	0.141	0.9	143	295	20	282
G20-2	OSIRIS	0.141	0.6	122	281	29	281
G20-2	GMOS + OSIRIS	0.141	0.7	121	309	19	277
SDSS 013527-1039	GMOS	0.127	1.3	120	424	55	467
SDSS 013527-1039	OSIRIS	0.127	1.0	118	404	53	429
SDSS 013527-1039	GMOS + OSIRIS	0.127	1.0	111	85	12	185
SDSS 234657+0056	GMOS	0.182	1.1	92	330	23	337
SDSS 234657+0056	OSIRIS	0.182	0.9	92	506	84	540
SDSS 234657+0056	GMOS + OSIRIS	0.182	0.7	85	404	41	428
COSMOS 127977	KMOS	1.62	3.4	215	3154	434	3242
COSMOS 127977	OSIRIS	1.62	4.7	248	3074	363	3045
COSMOS 127977	KMOS + OSIRIS	1.62	3.9	236	2532	227	2279
UDS 78317	KMOS	1.47	0.4	57	569	76	484
UDS 78317	OSIRIS	1.47	0.8	44	628	114	534
UDS 78317	KMOS + OSIRIS	1.47	0.2	29	338	64	200

Note. Columns: (1) galaxy identifier; (2) data source (natural seeing GMOS or KMOS, AO OSIRIS, or combination of natural seeing and AO); (3) redshift; (4) radius at which rotation curve becomes flat; (5) asymptotic velocity; (6) stellar specific AM; (7) measurement uncertainty in j_* ; (8) stellar specific AM using $\tilde{j}_* = kr v$. Note that only the galaxies with both natural and AO are presented in this table.

likely be attributed to the difference in PSFs of the two maps (0'.1 versus 0'.6). The corresponding AO velocity map is consistent with the seeing-limited classification of a rotating disc galaxy, but also reveals a kinematic twist along the minor axis that is not seen in natural seeing. In the case of UDS 78313, the finer PSF of the AO data uncovers additional substructure that is not evident in the seeing-limited data.

The rotation curves presented in Fig. 3 illustrate the complementarity of both natural seeing observations and AO-assisted data. The natural seeing velocity field of COSMOS 127977 is well fit by the model rotation curve in the top panel of Fig. 3, while the middle panel displays the additional structure revealed in the AO maps. Combining the two data sets as described in Section 3 leads to a more well-constrained model rotation curve (lower panel), and therefore a more accurate determination of total j_* . We reiterate that the model is only used to calculate j_i in the spaxels i where low signal to noise prohibits calculation from the data. The 2D spatial structure traced by the integral field data (i.e. by the AO-assisted maps in the inner regions of the galaxy and the seeing-limited maps in the outer regions where the AO data has low S/N) is used to calculate j_i elsewhere. The rotation curves for merger system UDS 78317 are in stark contrast to the well-behaved rotation curves of COSMOS 127977. None of the 1D velocity fields are well fit by model rotation curves; for this system there is no clear benefit to using any one of the three data sets in determining j_* .

Figs 4 and 5 show the normalized cumulative stellar specific AM $j_*(\leq r)/j_*$ in order to illustrate the degree of convergence, and the relative contribution to j_* made by the AO-assisted data, the natural seeing data and the model-informed estimate. We include the six

DYNAMO and two high- z galaxies for which we have both AO and seeing-limited observations. All eight qualitatively show a strong degree of convergence illustrated by the flatness of the cumulative j_* profile, owing to the large multiples of the disc radius $3.5 < r/r_d < 10$ observed. The horizontal, dashed and dotted lines in these figures correspond to the contribution of the AO, seeing-limited, and model spaxels as a fraction of total j_* ; on average 69, 18, and 13 per cent, respectively. Note that the intersection of the profile with these lines does not correspond to a strict radial cut, but can instead be interpreted as an approximate mean boundary to the physical region where the two data types and model *most strongly* contribute. For example, for C222 the AO-assisted data are most critical for $r/r_d \lesssim 2.75$, the seeing-limited data between $2.75 \lesssim r/r_d \lesssim 5.5$, and the model-informed estimate beyond $5.5 \lesssim r/r_d$. However, since the length of the x -axis r/r_d is set by the limit of the data, the observations contribute at radii as great as $r/r_d \lesssim 7.3$.

For comparison with our adopted spaxel-wise integration method we also compute the rotation curve model, adopting $\tilde{j}_* = 2v_{\text{flat}}r_d$, which is commonly used in studies of j_* large samples of galaxies at $z \sim 1.5$ (e.g. Swinbank et al. 2017). We include these values in Tables 1 and 2. Fig. 6 illustrates the percent difference between specific angular momenta measured with the two methods, $\Delta j_* = (j_* - \tilde{j}_*)/j_*$. Across all data sets, \tilde{j}_* differs from our two-dimensional integrated j_* by 6.75 per cent, which is less than the level of measurement uncertainty. The cases where \tilde{j}_* differs from our j_* by more than one standard deviation are the targets that have particularly clumpy morphology (e.g. G08-5, G20-2, SDSS 033244+0056) or where the kinematic map shows substructure (e.g. UDS 78317, which has the highest $\Delta j_* = 0.406$ for the combined AO + seeing-limited data set). Our primary motivation

Table 2. Adopted properties of DYNAMO and $z \sim 1.5$ galaxies.

Name	RA (hms)	Dec. (dms)	z	Obs	M_* ($\log(M_\odot)$)	$\Delta M_*/M_*$ (dex)	β	$\Delta\beta$
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
C22-2	22:39:49.34	−08:04:18.0	0.071	GMOS	10.34	0.20	0.10	0.05
D13-5	13:30:07.01	+00:31:53.2	0.075	GMOS+OSIRIS	10.65	0.20	0.02	0.05
G04-1	04:12:19.71	−05:54:48.6	0.130	GMOS+OSIRIS	11.01	0.20	0.10	0.05
G08-5	08:54:18.74	+06:46:20.5	0.132	GMOS	10.57	0.20	0.00	0.05
G10-1	10:21:42.47	+12:45:18.8	0.144	GMOS	10.44	0.20	0.08	0.05
G20-2	20:04:42.92	−06:46:57.9	0.141	GMOS+OSIRIS	10.61	0.20	0.14	0.05
SDSS 013527−1039	01:35:27.10	−10:39:38.6	0.127	OSIRIS	10.83	0.20	0.11	0.05
SDSS 024921−0756	02:49:21.42	−07:56:58.7	0.153	OSIRIS	10.48	0.20	0.73	0.05
SDSS 033244+0056	03:32:44.77	+00:58:42.1	0.182	GMOS	10.86	0.20	0.00	0.05
SDSS 212912−0734	21:29:12.15	−07:34:57.6	0.184	OSIRIS	10.85	0.20	0.00	0.05
SDSS 234657+0056	23:46:57.12	+00:56:28.9	0.182	GMOS+OSIRIS	10.79	0.20	0.05	0.05
COSMOS 127977	09:59:37.961	02:18:02.16	1.62	KMOS+OSIRIS	10.77	0.20	0.00	0.10
UDS 78317	02:17:34.193	−05:10:16.61	1.47	KMOS+OSIRIS	10.32	0.20	0.00	0.10

Name	r_d (kpc)	r_{flat} (kpc)	v_{flat} (km s^{-1})	j_* (kpc km s^{-1})	Δj_* (kpc km s^{-1})	\tilde{j}_* (kpc km s^{-1})	σ (km s^{-1})	$\Delta\sigma$ (km s^{-1})
(1)	(10)	(11)	(12)	(13)	(14)	(15)	(16)	(17)
C22-2	1.5	1.3	164	449	53	498	32	5
D13-5	1.3	0.4	171	466	51	437	46	5
G04-1	2.3	0.7	221	991	118	1025	50	5
G08-5	1.3	0.5	248	733	65	660	64	5
G10-1	3.2	1.1	118	670	105	756	52	3
G20-2	1.1	0.7	121	309	19	277	81	5
SDSS 013527−1039	1.8	1.0	118	404	53	429	41	5
SDSS 024921−0756	1.1	0.4	84	188	31	185	57	5
SDSS 033244+0056	1.5	0.7	239	804	59	695	59	5
SDSS 212912−0734	1.5	0.6	101	317	47	303	53	5
SDSS 234657+0056	2.5	0.7	85	404	41	428	–	–
COSMOS 127977	4.8	3.9	236	2532	227	2279	57	11
UDS 78317	3.5	0.2	29	338	64	200	60	23

Notes. Columns: (1) galaxy identifier; (2) right ascension (J2000); (3) declination (J2000); (4) redshift; (5) adopted data source (natural seeing GMOS or KMOS, AO OSIRIS, or combination of natural seeing and AO); (6) base 10 logarithm of stellar mass; (7) measurement uncertainty in M_* ; (8) bulge-to-total ratio; (9) measurement uncertainty in β ; (10) exponential disc scale length; (11) radius at which rotation curve becomes flat; (12) asymptotic velocity; (13) stellar specific AM; (14) measurement uncertainty in j_* ; (15) approximate stellar specific AM using $j = kr_v$; (16) velocity dispersion; (17) measurement uncertainty in σ .

for adopting the spaxel-wise integration method described above is to account for the diversity of galaxies such as these. The result can be interpreted to mean that j_* measured from spaxel-wise integration and \tilde{j}_* measured from the rotation curve model method in general give consistent results.

We now consider the systematic effects of the three different data sets (GMOS, OSIRIS, KMOS as well as DYNAMO versus $z \sim 1.5$ galaxies). As discussed above these different sets vary in both radial coverage of the velocity profile and spatial resolution, which can be important for tracing the bulk of AM. We will consider both the effect on measurement uncertainties and the systematic effects on the value of total j_* across data type. In Table 3, we compare the three data sets for COSMOS 127977, UDS 78317 and the six DYNAMO galaxies for which we have both natural seeing and AO data.

Overall there is a general decrease in median measurement uncertainty Δj_* as more information is included in the fit, as one would expect for random noise. For COSMOS 127977, the measurement uncertainty decreases from 14 per cent with KMOS-only to 9 per cent when the OSIRIS and KMOS data is combined. However, in UDS 78317 the measurement uncertainty increases

from 13 per cent for KMOS-only to 18 per cent for the combined measurement. This is due to additional substructure being detected with OSIRIS, as illustrated in Figs 1 and 2.

The DYNAMO sample median uncertainty on j_* decreases from 13 per cent (GMOS-only) or 16 per cent (OSIRIS) to 10 per cent for the combined data set. The higher median uncertainty for AO than natural seeing in DYNAMO could be an artefact of finer resolution of clumps,⁴ and lower signal to noise at high multiples of r_e , both of which mean the model fit is less certain, which in turn contributes to uncertainty in j_* . Our philosophy to adopt in general the data set with the most data results in selecting the data set that has the lowest relative measurement uncertainty on j_* . For C22-2 and SDSS 013527-1039, where we respectively adopt seeing-limited and AO-only data, the relative measurement uncertainty on j_* is 1.7 and 0.2 per cent larger, respectively.

⁴This is assuming that the clumps have their own velocity field which disturbs the velocity field of the galaxy (as seen in simulations e.g. Ceverino et al. 2012, but not yet seen in observations).

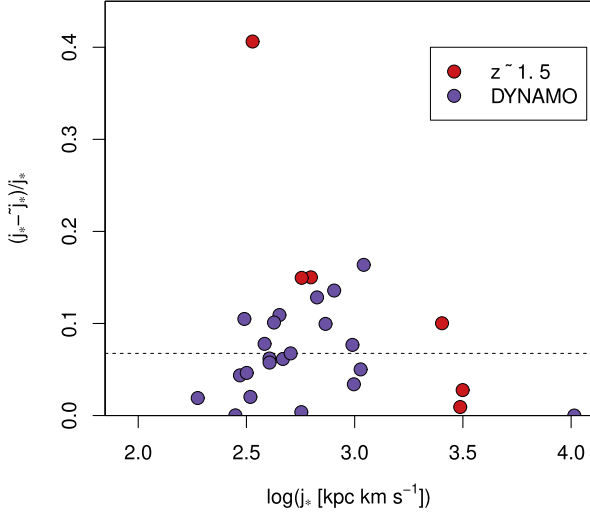


Figure 6. Comparison of specific AM measured from spaxel-wise integration (j_*) with those measured via the commonly used rotation curve model method (\tilde{j}_*). The fractional difference is calculated with $(j_* - \tilde{j}_*)/j_*$. Measurements using all three data sets (AO-assisted, seeing-limited, combination) are shown. The horizontal line represents the mean fractional difference.

Table 3. Median j_* and uncertainty in j_* for natural, AO, and natural + AO data.

	Natural seeing	Adaptive optics	Natural + AO
$z \sim 1.5$			
$\log(j_*)$	3.50 ± 0.06	3.49 ± 0.05	3.4 ± 0.04
$\Delta j_*/j_*$	0.14	0.12	0.09
$z \sim 0$			
$\log(j_*)$	2.64 ± 0.24	2.73 ± 0.10	2.60 ± 0.14
$\Delta j_*/j_*$	0.13 ± 0.02	0.16 ± 0.01	0.10 ± 0.01

Using the OSIRIS data on its own can sometimes give dramatically different values of j_* , due to the more restricted coverage of the velocity field compared with GMOS or KMOS. For example, UDS 78317 j_* measured with OSIRIS is a factor of 2 higher than the combined KMOS + OSIRIS data set. The KMOS-only measurements at $z \sim 1.5$ in general disagree with the combined KMOS + OSIRIS by at least 20 per cent. For UDS 78317, the disagreement in j_* is at the 60 per cent level. We note that the seeing-limited data are consistent with a rotating disc, but the H α intensity maps and ‘multipolar’ velocity maps together indicate that this may be two rotating galaxies undergoing a merger. It is possible that using kinemetry (Krajnović et al. 2006) or modelling (Rodrigues et al. 2017) may be able to identify this system as a merger in the KMOS data, however this is beyond the scope of this paper. The implication from our detailed observations of these two $z \sim 1.5$ galaxies is that the systematic uncertainty on j_* is at best 20 per cent, and in some cases may be significantly higher. While we acknowledge that our sample is small, none the less we recommend that caution should be taken when interpreting j_* that is measured with only natural seeing at $z > 1$.

The GMOS-only measurements can be thought of as analogous to the KMOS+OSIRIS data set at $z \sim 1.5$. Both AO enabled

observation with OSIRIS at $z \sim 1.5$ and the seeing-limited (~ 0.5 – 0.7 arcsec) observations of DYNAMO galaxies with GMOS offer a resolution in the central part of the rotation curve of order ~ 1 kpc. Moreover, both data sets reach sufficiently far in radius to adequately constrain the flat rotation curve. Observations of DYNAMO galaxies that include OSIRIS offer finer spatial resolution that what is available on unlensed galaxies at $z \gtrsim 1$. We can therefore use this comparison to understand what information is lost on measurements of j_* on $z \gtrsim 1$ galaxies.

With the exception of one target (D13-5), the j_* values of GMOS-only observations of DYNAMO galaxies agree with the corresponding GMOS + OSIRIS values to the 11 per cent level. The values of j_* for D13-5 are a factor of 2 higher in the GMOS-only data than in the combined GMOS + OSIRIS data. This discrepancy arises because the seeing-limited data are not well fit by the exponential disc model used for extrapolation. We note that this measurement has the highest measurement uncertainty (20 per cent) in our sample. When combining the data, the low S/N GMOS spaxels are replaced by OSIRIS, so the combination is well fit. We interpret this to indicate that the general correspondence between GMOS-only and GMOS + OSIRIS in DYNAMO galaxies indicates that using KMOS + OSIRIS at $z \sim 1.5$ is sufficient to achieve a robust result in that using finer spatial resolution would not appreciably alter the measurement of j_* .

The consequence is that high-redshift studies that utilize only natural seeing observations, or only AO-assisted data, in general are likely to measure less well-constrained j_* than if using a combination of seeing-limited and AO-assisted data, and may also marginally overestimate j_* . One might expect that effect of using only natural seeing data would be to *underestimate* j_* due to beam smearing, but since our natural seeing data are scaled for beam smearing we do not see that effect here.

5 THE RELATION BETWEEN STELLAR MASS, SPECIFIC ANGULAR MOMENTUM, AND MORPHOLOGY

In this section, we analyse the relationship between stellar mass, specific AM, and morphology of $z \sim 1.5$ galaxies and their local analogues in the DYNAMO sample, compared with normal local galaxies from THINGS, CALIFA, and RF12 as presented in Sweet et al. (2018a), in order to quantify how bulge growth and disc stability are correlated with the build-up of AM and stellar mass M_* . We use our full DYNAMO sample (i.e. we include the galaxies for which we have only seeing-limited data, those for which we only have AO-assisted data, and those for which we have both) since there is likely to be no significant systematic effect on stellar specific AM j_* as demonstrated in Section 4.

The $M_* - j_*$ plane is shown in Fig. 7. DYNAMO galaxies all lie below the 2D relation for normal local disc galaxies, in the region occupied by normal galaxies with moderate ($\beta \sim 0.4$) bulge fraction. There is a large amount of scatter, likely due to the range of specific star formation rates and consequent range of star formation-induced turbulence, which is connected via disc stability to a corresponding range in j_* . The $z \sim 1.5$ disc galaxy COSMOS 127977 is consistent with local L_* galaxies, with a large $j_* = 2500 \pm 200$ kpc km s $^{-1}$ and $\log(M_*/M_\odot) = 10.77$. The merging system at $z \sim 1.5$, UDS 78317, lies below the $M_* - j_*$ relation amongst the DYNAMO sample. We point out that, since the system is not in dynamical equilibrium, the assumptions made in determining j_* in this manner are not valid, so this measurement may not be meaningful.

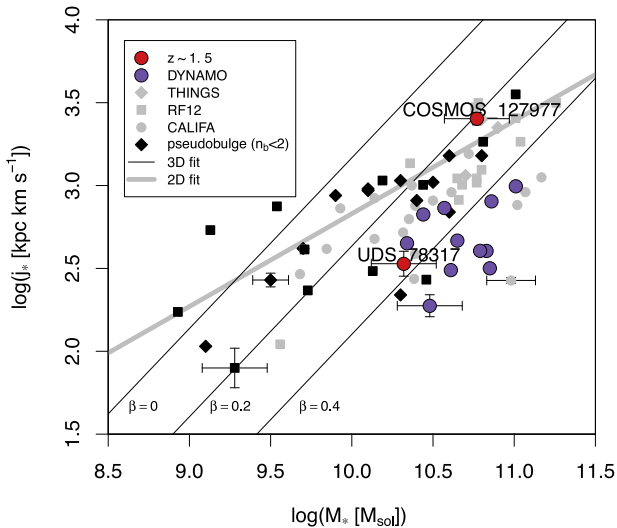


Figure 7. The relation between stellar mass M_* and stellar specific AM j_* for the two $z \sim 1.5$ galaxies (red filled circles) and the local analogue DYNAMO galaxies (purple filled circles), overlaid on the results for normal local disc galaxies (grey and black diamonds, squares, and small circles) presented in Sweet et al. (2018a). The DYNAMO galaxies occupy the low- j_* region occupied by moderately bulge-dominated local galaxies, but themselves have low bulge fraction β . COSMOS 127977 has a high j_* for its stellar mass and is consistent with local spirals. UDS 78317 lies within the DYNAMO scatter, but the OSIRIS observations reveal that this system is a merger.

Motivated by the empirical finding by OG14 and S18 that the 3D fit

$$\frac{j_*}{10^3 \text{ kpc km s}^{-1}} = ke^{(-g\beta)} \left(\frac{M_*}{10^{10} M_\odot} \right)^\alpha, \quad (3)$$

yields $\alpha \sim 1$, and the physical interpretation that $j_*/M_* = J_*/M_*^2$ is connected with disc stability (Obreschkow & Glazebrook 2014; Romeo & Mogotsi 2018), we show the $\beta - j_*/M_*$ plane in Fig. 8. This figure illustrates that the location of UDS 78317 and the DYNAMO galaxies on Fig. 7 cannot simply be explained by high β , since these systems do not have large bulges. They all have low β for their ratio of j_* to M_* compared with the relation for normal local disc galaxies that host pseudo-bulges, presented in Sweet et al. (2018a). COSMOS 127977 is within the scatter of the local control samples owing to its high j_* . If our assumption that the gas and stars corotate is incorrect for this $z \sim 1.5$ galaxy as discussed in Footnote 2, then its $\log(j_*/M_*)$ would be overestimated by 0.1 dex, moving it marginally below the scatter of the local control samples but still above the turbulent DYNAMO systems.

We investigate the relation between degree of turbulence and distance from the $\beta - j_*/M_*$ relation along the β axis in Fig. 9. The degree of turbulence is quantified by the ratio of velocity dispersion σ to rotational velocity v_{flat} , which is shown to correlate with clump size in Fisher et al. (2017a). It stands to reason that clump size correlates with mass as clumps have relatively constant surface brightness both in H α emission (Fisher et al. 2017b) and stellar mass (Cava et al. 2018). In this sense σ/v_{flat} is an accessible proxy for clumpiness. There are two separate groups on this plot, where turbulent DYNAMO and $z \sim 1.5$ galaxy COSMOS 127977 have a larger offset from the $\beta - j_*/M_*$ relation than regular local THINGS galaxies, which have low dispersion. σ/v_{flat} for UDS 78317 is too high for that galaxy to appear on this figure, but this is not unexpected, since as a merging system its v_{flat} does not correspond to

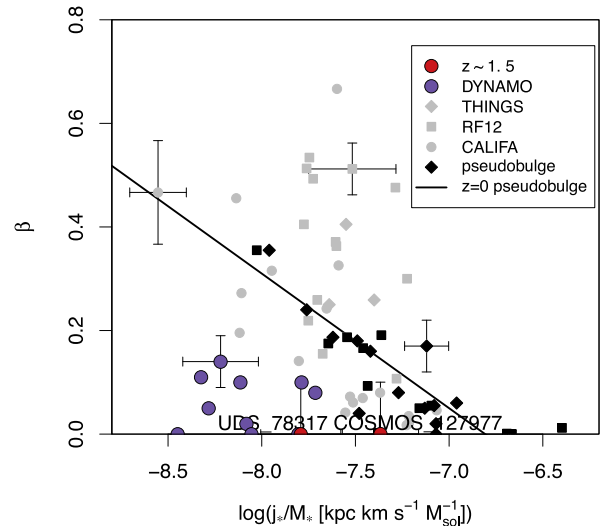


Figure 8. The relation between bulge fraction β and stellar specific AM per unit stellar mass j_*/M_* for the two $z \sim 1.5$ galaxies and the local analogue DYNAMO galaxies, overlaid on the results for normal local disc galaxies presented in Sweet et al. (2018a). The DYNAMO galaxies are offset from the relation defined by local galaxies that host pseudo-bulges, with relatively small bulges for their j_*/M_* ratios. COSMOS 127977 is also below the local relation, but within the dispersion of the local sample. UDS 78317 is consistent with the highest j_*/M_* DYNAMO galaxies.

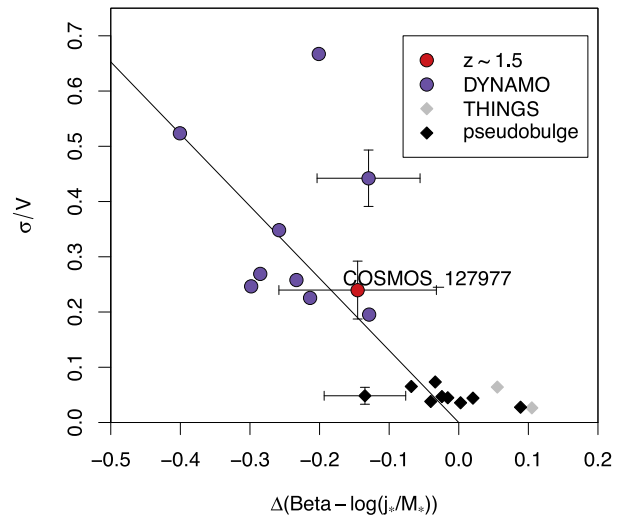


Figure 9. The relation between the offset to $\beta - j_*/M_*$ relation and ratio of velocity dispersion to rotational velocity σ/v_{flat} for the $z \sim 1.5$ galaxy COSMOS 127977 and the local analogue DYNAMO galaxies, overlaid on the results for normal local disc galaxies THINGS presented in Sweet et al. (2018a). DYNAMO galaxies and COSMOS 127977 are offset from THINGS galaxies.

that of a rotating disc. The implied result of the broad trend between clumpiness and offset from $\beta - j_*/M_*$ is that galaxies that deviate further from the pseudo-bulge relation are still in the process of building their bulges. Interestingly, high- z galaxy COSMOS 127977 is consistent with local analogue DYNAMO galaxies only once its turbulence is accounted for, suggesting that ignoring this parameter can yield an incomplete picture of galaxy evolution.

6 DISCUSSION

In this section, we discuss the potential evolution of DYNAMO galaxies in $M_*-j_*-\beta$ space, and compare the resulting implications for high- z galaxies with our findings at $z \sim 1.5$.

We have seen in the previous section that DYNAMO galaxies have low j_* for a given stellar mass, occupying the space generally populated by early-type galaxies. However, unlike early types, DYNAMO galaxies do not have a large central bulge and are clumpy and turbulent, representing an earlier stage of evolution than typical local disc galaxies. The DYNAMO galaxies exhibit a large scatter, but this is not due to the inclusion of present-day mergers, since this sample excludes systems that do not appear to be discs (i.e. those with disturbed velocity maps and/or non-exponential surface brightness profiles).⁵ The scatter can be at least partially attributed to the range in star formation properties, noting that they have specific star formation rates consistent with galaxies between $0 \lesssim z \lesssim 2$ (e.g. C22-2 is consistent with other $z = 0$ galaxies). If the clumps in these galaxies remain bound and migrate to the centre, as proposed in Ceverino et al. (2012), then perhaps the mass of the clumps could build the bulge mass, and these high- z analogues may evolve to reach the present-day relation traced by pseudo-bulges in Fig. 8. For three of these targets (D13-5, G04-1, and G20-2), data presented in Fisher et al. (2017a) can be used to make a back-of-envelope calculation of future bulge fraction $\beta_{\text{future}} = (M_{\text{clump}} + \beta M_*) / (M_* + M_{\text{clump}})$, where $M_{\text{clump}} = \text{SFR}_{\text{clump}} t_{\text{dep}}$ is the clump mass available to build the bulge, $\text{SFR}_{\text{clump}}$ is the total star formation rate in the clumps, t_{dep} is the depletion time for the galaxy, β is the current bulge fraction, and M_* is the current stellar mass of the galaxy. The future bulge fractions projected in this way for D13-5, G04-1, and G20-2 are $\beta_{\text{future}} = 0.19, 0.24,$ and 0.25 , respectively. These estimates move these three galaxies into the range of the pseudo-bulge relation in Fig. 8, indicating that the clumps could contribute to building up the bulges, though perhaps not on their own. Additionally, if there was future gas accretion there would need to be subsequent secular evolution to keep these galaxies on the pseudo-bulge relation. We have a current (Cycle 25) *HST* program (PI: Fisher) to measure clump stellar masses, which will improve these estimates. In a future paper, we will investigate whether or not summing the mass of the clumps with the bulge is sufficient to relocate DYNAMO galaxies to the pseudo-bulge relation, or whether there is some additional mechanism required.

Now, the distance to the pseudo-bulge relation is generally correlated with degree of turbulence, quantified as σ/v_{flat} , where σ is not from thermal pressure alone but also from turbulence pressure due to star formation. In the case of DYNAMO galaxies, these gas-rich, turbulent discs represent an earlier stage in evolution and have not yet built up their bulges. The contribution from star formation-induced turbulence is high owing to the large clumps and high star formation rates, so σ/v_{flat} is a proxy for clumpiness. As the DYNAMO galaxies evolve towards the pseudo-bulge track, they move to the right of Fig. 9, so they must also decrease their σ/v_{flat} in order to remain consistent with the trend shared with normal local galaxies. This would require star formation to decrease and the disc to settle as they move closer to the pseudo-bulge track and become more like typical present-day disc galaxies. The corollary is that the pseudo-bulge relation breaks down for clumpy galaxies, and should not be used at $z \gtrsim 1$.

⁵There may still be remnants of past mergers in the sample, since past gas-rich mergers would leave disky, bulge-less systems (Hopkins et al. 2009).

There is still the outstanding question as to why high- z -like discs exist today, since their clumpy nature and low AM do not necessarily follow from their high star formation rates by which they were selected. They may have formed in the high-redshift Universe and have somehow survived in their clumpy, bulgeless form to the present day, evolving less than their counterparts owing to a relatively underdense environment. Alternatively they may have formed more recently, but in unique environments where the conditions resemble those in the denser, earlier Universe. Analysis of their environments and stellar ages may help to distinguish between these scenarios.

If we assume that DYNAMO galaxies are in fact analogues of galaxies at $0 \lesssim z \lesssim 2$, then comparing to typical local galaxies in THINGS can be informative about the redshift evolution of j_* . For DYNAMO in this work and O15 we see low j_*/M_* ⁶ and low β , suggesting that discs at $z \sim 1.5$ are likewise in general less stable than at $z \sim 0$. The enhanced star formation-induced turbulence in DYNAMO – which (together with gas fraction, high dispersion, disky nature, compactness, and clumpiness) earns that sample the ‘high- z analogue’ label, since it is also the case in high- z discs – is consistent with this picture.

It is instructive to confirm the above discussion, where we treat DYNAMO galaxies as local analogues of clumpy high- z discs, with high-quality observations of systems at $z \sim 1.5$. Interestingly, neither of the two $z \sim 1.5$ galaxies presented here matches this description. COSMOS 127977 is consistent with typical $z \sim 0$ discs in M_*-j_* and $\beta-j_*/M_*$ space, even though it has an enhanced σ/v_{flat} compared with local THINGS galaxies by virtue of its bright, star-forming clumps. Inclusion of the σ/v_{flat} turbulence parameter is necessary to see its expected correspondence with local analogues, suggesting that this is an important parameter in understanding galaxy evolution. We note that COSMOS 127977 was selected for observation based on the seeing-limited KGES data. The KGES $z \sim 1.5$ sample exhibits a wide range of rotational velocity and angular size. For this pilot work, we pre-selected galaxies (1) that show evidence of rotation in KGES, to ensure a high-quality j_* measurement despite the challenges of observing at such high redshift and (2) that maximally occupy half of the OSIRIS field of view, to facilitate on-detector beam-switching sky subtraction and sampling with as many resolution elements as possible. This selection is consequently biased towards higher j_* and larger effective radius, thus also to higher M_* . COSMOS 127977 may be a more evolved system than most $z \sim 1.5$ galaxies, in the sense that it has experienced the right conditions for its disc to settle and j_* to build up, bringing it nearer the pseudo-bulge relation.

The other $z \sim 1.5$ system in our sample, UDS 78317, appears to be a merging system, so is not a normal $z \sim 1.5$ disc either, even though it is consistent with local analogues of high- z galaxies in terms of j_* , M_* , β , and σ/v_{flat} , and would seem to confirm the above evolutionary discussion. This raises important points about the effect of image quality on merger/disc interpretation and subsequent ill-advised inclusion of mergers as though they were rotating discs. UDS 78317 appears to be a rotating disc in the seeing-limited data, with the intensity and velocity maps showing no obvious sign that this system may be a merger (excluding more detailed analysis such as

⁶We remind the reader that analysing this ratio (rather than j_* or $j_*/M_*^{2/3}$) is motivated by OG14 and S18, who find that the slope of the M_*-j_* relation $\alpha \sim 1$ for fixed β ; OG14 make the physical interpretation that $j_*/M_* = J_*/M_*^2$ is connected with disc stability, but see also Romeo & Mogotsi (2018).

kinemetry). It is only with the enhanced PSF of the AO maps, which reveal that the system is clumpy and disturbed, that one realizes that UDS 78317 may in fact be a merging system and cannot be treated as a rotating disc galaxy. This is supported by the SINS/zC-SINF AO survey (Förster Schreiber et al. 2018), who made a comparison between deep AO and non-AO data for 34 galaxies at $z \sim 2$. They found that the larger (angular size) sources were broadly consistent between the two data sets, but that for 14 of the 17 smaller, less resolved sources, the AO maps tended to either further resolve clumps (in six objects) or resolve new structure (in eight objects), including minor mergers in three cases. Rodrigues et al. (2017) found this to be more serious for KMOS3D at $z \sim 1$, with mergers being misclassified as rotating disc galaxies in 50 per cent of cases. We note that gas-rich mergers at high redshift have been shown to evolve to resemble disc-like systems at late times, with a range of final AM depending on the AM vectors of the merging components (Robertson et al. 2006). We suggest that some fraction of the scatter in $M_* - j_*$ presented by other studies at high redshift may thus be driven by including a greater number of mergers as if they were rotating discs; this could be checked by measuring j_* in the manner described in the current paper for the SINS/zC-SINF AO and non-AO data sets. Most other high- z studies (Förster Schreiber et al. 2006; Burkert et al. 2016; Contini et al. 2016; Harrison et al. 2017; Swinbank et al. 2017) find that $j_* \propto M^{2/3}$ for the 2D relation [with the exception of Alcorn et al. (2018), who found a shallower slope, but note that they compute j_* from integrated spectra]. However, the normalization of this relation leads to a wide range of conclusions about the redshift evolution $(1+z)^n$, ranging from $n = 0$ (Burkert et al. 2016; Alcorn et al. 2018) to $n = -1.5$ (Förster Schreiber et al. 2006). Some of this variation may be due to the inclusion of current mergers, and other sample selection differences. We also note that these works assume a smooth disc with simple model $j = kr v$ instead of utilizing the spatially resolved, 2D maps as we do in this paper. If we perform a similar calculation adopting $\tilde{j}_* = 2v_{\text{flat}} r_d$ assuming pure discs, then \tilde{j}_* is lower than our integrated j_* by 11 and 40 per cent for COSMOS 127977 and UDS 78317, respectively. This is likely to further increase the scatter in j_*/M_* in those samples (also see Obreschkow & Glazebrook 2014), and may also affect the normalization.

We are gathering a larger, more representative sample of natural + AO observations of $z \sim 1.5$ discs to quantify the location of high- z galaxies in $M_* - j_*$ and $\beta - j_*/M_*$ space in an accurate, self-consistent manner.

7 CONCLUSIONS

In this paper we have presented high-quality specific AM measurements for local turbulent galaxies in DYNAMO and two $z \sim 1.5$ systems, using a novel combination of AO-assisted and seeing-limited data. We make the following points.

(i) Image quality affects specific AM, in that combining fine PSF of AO-assisted observations in the central regions with high signal to α ise of seeing-limited data in the outskirts leads to a more well-constrained j_* . The mean measurement uncertainty $\Delta j_*/j_*$ is reduced from 13 per cent with seeing-limited data or 16 per cent with AO alone to 10 per cent in the combination of the two data types. The high-quality j_* measured in this manner may be marginally lower than j_* measured with just one type of data or the other.

(ii) In particular, high- z galaxies observed only in natural seeing may be misclassified as disc galaxies when they are in fact merging systems. Such systems may appear to be consistent with local

analogues of high- z galaxies and with theoretical expectations, but cannot be sensibly compared with them. Some of the scatter in $M_* - j_*$ and $\beta - j_*/M_*$ space may be driven by inclusion of merging systems as though they were rotating disc galaxies.

(iii) Local analogues of high- z galaxies have low j_* for their M_* , but also lie below the $\beta - j_*/M_*$ relation for normal local galaxies that host pseudo-bulges of Sweet et al. (2018a). Their offset from that relation is broadly correlated with and possibly explained by a physical model whereby enhanced σ/v_{flat} is contributed by star formation-induced turbulence.

(iv) COSMOS 127977, a disc galaxy at $z \sim 1.5$, is consistent with normal local disc galaxies in terms of j_* , M_* , and β , albeit with enhanced σ/v_{flat} . It may be a more evolved system than typical discs at $z \sim 1.5$ and represent an intermediate phase between low- j_* turbulent discs and today's high- j_* , smooth galaxies.

In future papers, we will extend this work to a larger sample of high- z galaxies and present detailed analyses of spatially resolved PDF(j_*) (Gillman et al. 2019, Sweet et al. 2018b).

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