
Available from: http://dx.doi.org/10.1111/j.1745-3933.2009.00723.x

Copyright © 2009 The authors.

This is the author’s version of the work, posted here with the permission of the publisher for your personal use. No further distribution is permitted. You may also be able to access the published version from your library. The definitive version is available at www.interscience.wiley.com.
Spin-down rate and inferred dipole magnetic field of the soft gamma-ray repeater SGR 1627–41

P. Esposito,1,2* M. Burgay,3 A. Possenti,3 R. Turolla,4,5 S. Zane,5 A. De Luca,1,6 A. Tiengo,1 G. L. Israel,7 F. Mattana,8 S. Mereghetti,1 M. Bailes,9 P. Romano,10 D. Götz,11 and N. Rea12,13

1INAF/Istituto di Astrofisica Spaziale e Fisica Cosmica - Milano, via E. Bassini 15, 20133 Milano, Italy
2Istituto Nazionale di Fisica Nucleare, Sezione di Milano, via O. Raimondo 4, I-20133 Milano, Italy
3INAF/Osservatorio Astronomico di Cagliari, località Poggio dei Pini, strada 54, 09012 Capoterra, Italy
4Universität des Studi Padova, Dipartimento di Fisica, via F. Marzolo 8, 35131 Padova, Italy
5INAF/Osservatorio Astronomico di Roma, via Frascati 33, 00040 Monteporzio Catone, Italy
6Mullard Space Science Laboratory, University College London, Holmbury St. Mary, Dorking, Surrey RH5 6NT, UK
7IUSS - Istituto Universitario di Studi Superiori, viale Lungo Ticino Sforza 56, 27100 Pavia, Italy
8INAF/Osservatorio Astronomico di Roma, via Molinettone 101, 00133 Roma, Italy
9INAF/Istituto di Astrofisica Spaziale e Fisica Cosmica - Palermo, via U. La Maia 153, 90146 Palermo, Italy
10Istituto Nazionale di Fisica Nucleare, Sezione di Pavia, via A. Bassi 6, 27100 Pavia, Italy
11Centre for Astrophysics and Supercomputing, Swinburne University of Technology, PO Box 218, Hawthorn, VIC 3122, Australia
12University of Amsterdam, Astronomical Institute Anton Pannekoek, Kruislaan 403, 1098 SJ Amsterdam, The Netherlands
13CSIC - Institut d’Estudis Espacials de Catalunya, Campus UAB, Fac. Ciències, Torre C5 parell 2, 08193 Bellaterra, Spain

* E-mail: paoloesp@iasf-milano.inaf.it
1 Ten AXPs and six SGRs are confirmed, and there are a few candidates; see catalog at http://www.physics.mcgill.ca/~pulsar/magnetar/main.html.

ABSTRACT

Using Chandra data taken on 2008 June, we detected pulsations at 2.59439(4) s in the soft gamma-ray repeater SGR 1627–41. This is the second measurement of the source spin period and allows us to derive for the first time a long-term spin-down rate of $1.9 \pm 0.4 \times 10^{-11}$ s s$^{-1}$. From this value we infer for SGR 1627–41 a characteristic age of $\sim 2$ kyr, a spin-down luminosity of $\sim 4 \times 10^{34}$ erg s$^{-1}$ (one of the highest among sources of the same class), and a surface dipole magnetic field strength of $\sim 2 \times 10^{14}$ G. These properties confirm the magnetar nature of SGR 1627–41; however, they should be considered with caution since they were derived on the basis of a period derivative measurement made using two epochs only and magnetar spin-down rates are generally highly variable. The pulse profile, double-peaked and derived on the basis of a period derivative measurement made using two epochs only and magnetar spin-down rates are generally highly variable. The pulse profile, double-peaked and associated with a pulsation fraction of $\pm 2\%$ in the 2–10 keV range, closely resembles that observed by XMM-Newton in 2008 September. Having for the first time a timing model for this SGR, we also searched for a pulsar signal in archival radio data collected with the Parkes radio telescope nine months after the previous X-ray outburst. No evidence for radio pulsations was found, down to a luminosity level $\sim 10^{9}$ times fainter (for a 10% duty cycle and a distance of 11 kpc) than the peak luminosity shown by the known radio magnetars.

Key words: pulsars: general – stars: neutron – X-rays: individual: SGR 1627–41.

1 INTRODUCTION

Anomalous X-ray pulsars (AXPs) and soft gamma-ray repeaters (SGRs) are isolated neutron stars with periods of several seconds ($P \sim 2–12$ s), rapid spin down ($\dot{P} \sim 10^{-11}$ s s$^{-1}$), bright ($\sim 10^{34}$–$10^{35}$ erg s$^{-1}$) and highly variable X-ray emission. AXPs and SGRs are commonly interpreted in terms of the magnetar model. Magnetars are ultra-magnetized neutron stars with magnetic fields largely in excess of the quantum critical field $B_{\text{QED}} = \frac{m_{e}^{2}c^{3}}{\pi^{2}h^{2}e^{2}} \sim 4.4 \times 10^{13}$ G (Paczynski 1992, Duncan & Thompson 1992, Thompson & Duncan 1995, 1996). Contrary to what happens in ordinary radio pulsars, the X-ray luminosity is larger than their rotational energy loss. Since no stellar companions have been detected thus far, also accretion is unlikely to be responsible for the emission of AXPs and SGRs. Their persistent X-ray luminosity, as well as the bursts and flares typical of these sources, are instead believed to be powered by the decay of their ultra-strong magnetic field (see Woods & Thompson 2006 and Mereghetti 2008 for recent reviews).

AXPs were first recognised as a class of persistent X-ray
pulsars, with the peculiarity that the X-ray luminosity exceeds that available from spin-down (whence the name “anomalous”; Mereghetti & Stella [1998]). SGRs were first noticed as hard-X-ray transients (Laros et al. 1987), characterized by recurrent, short (<1 s) and relatively soft (peak photon energy ∼25–30 keV) flashes with super-Eddington luminosity. Although SGRs and AXPs have been discovered through very different channels, observations performed over the last few years highlighted several similarities among these two classes of objects and pointed towards a common magnetar nature (see e.g. Rea et al. 2008). In particular, short and hard X-ray bursts, originally considered as the defining characteristic of SGRs, have now been observed in several AXPs (see e.g. Gavriil, Kaspi, & Woods 2002; Mereghetti et al. 2009).

SGR 1627–41 was discovered in 1998, when about one hundred bursts in six weeks were observed by CGRO/BATSE and other instruments (Woods et al. 1999). Its soft X-ray counterpart was identified with BeppoSAX in 1998 at a luminosity level of ∼10^{35} erg s^{-1} (Woods et al. 1999). Subsequent observations carried out with BeppoSAX, ASCA, Chandra, and XMM-Newton showed a spectral softening and a monotonic decrease in the luminosity, down to a level of ∼10^{34} erg s^{-1} (Kouveliotou et al. 2003; Mereghetti et al. 2006; Esposito et al. 2008).

After nearly ten years of quiescence, SGR 1627–41 re-activated on 2008 May 14, when several bursts were detected by Swift/BAT and other hard X-ray instruments (Esposito et al. 2008). The burst re-activation was associated with a large enhancement of the soft X-ray flux and a marked spectral hardening.

Until very recently, SGR 1627–41 was the only magnetar candidate with no pulsation period known. In order to search in depth for pulsations taking advantage of the high flux state, we asked for a long XMM-Newton observation to be carried out during its outburst. The observation was performed on 2008 September 27–28 and we could detect a clear pulsation period of 2.594 ± 0.000 04 s (Esposito et al. 2009). However, no meaningful constraints on the period derivative could be derived from that observation.

Here we report on a new measurement of the period using data gathered shortly after the burst activation by the Chandra X-ray Observatory. This allows us to estimate for the first time the spin-down rate of SGR 1627–41 and to infer its magnetic field, characteristic age, and spin-down luminosity. Taking advantage of the new pieces of information about the timing properties of SGR 1627–41, we also searched for a pulsed signal in archival radio data collected at the Parkes observatory.

2 THE CHANDRA OBSERVATION: DATA ANALYSIS AND RESULTS

The Chandra X-ray Observatory (Weisskopf et al. 2000) pointed its mirror towards SGR 1627–41 on 2008 June 3 (MJD 54620) and observed the source for about 40 ks (observation identifier: 9126). The observation was carried out with the Advanced CCD Imaging Spectrometer (ACIS; Garmire et al. 2003) instrument operated in the Continuous Clocking (CC) mode, which provides a time resolution of 2.85 ms and imaging along a single direction. The event telemetry was in Faint mode. The source was positioned in the back-illuminated ACIS-S3 chip, sensitive to photons in the 0.2–10 keV energy range.

The data were processed using the Chandra Interactive Analysis of Observation software (CIAO, version 4.1) and we employed the most updated calibration files available at the time the reduction was performed (CALDB 4.1). Standard screening criteria were applied in the extraction of scientific products. No significant background flares affected the observation.

The source photons for the timing and spectral analyses were accumulated from a 5 × 5 pixels region centred on SGR 1627–41 (one ACIS-S pixel corresponds to 0.7492); the background events were extracted from source-free regions of the same chip as the source. A total of about 1120 ± 40 counts above the background were collected from SGR 1627–41 in the 2–10 keV energy range.

2.1 Spectroscopy

The ancillary response file and the redistribution matrix for the spectral fitting were generated with the CIAO tasks ASPHIST, MKarf, and Mkacisrmf, using the specific bad-pixel file of this observation. The data were grouped with a minimum of 20 counts per energy bin and the spectrum was analysed with the XSPEC version 12.4. analysis package (Arnaud 1996).

Given the paucity of counts, we fit a simple model to the data: a power law corrected for interstellar absorption. We obtained the following best-fit parameters (χ^2 = 1.13 for 51 degrees of freedom): absorption N_H = 10^{21.1} × 10^{22} cm^{-2} and photon index Γ = 1.0^{+0.3}_{-0.2} (here and in the following all errors are at 1σ confidence level). The absorbed 2–10 keV flux was ∼1.3 × 10^{-12} erg cm^{-2} s^{-1}, corresponding to a luminosity of ∼3 × 10^{34} erg s^{-1}. These results are consistent with those reported in Woods et al. (2008) and confirm the bright and hard state of the source following the 2008 May 28 burst activation (Esposito et al. 2008; 2009).

2.2 Timing

For the timing analysis, the photon arrival times were converted to the Solar System barycentre with the CIAO tasks XBARBY using the source coordinates reported in Wachter et al. (2004). We searched for the presence of a periodic signal using a Z_2^p test (see Esposito et al. 2009) over the period range 2.58471–2.59460 s; this range was determined by extrapolating from the 3σ lower limit on the value reported in Esposito et al. (2009), conservatively assuming a period derivative of 0 ≤ P' ≤ 10^{-9} s^{-1}. The period search step size was ∼8 × 10^{-6} s, which is equivalent to oversampling the Fourier period resolution (2 P^2/T_{obs}) by a factor of 10.

A significant signal was found in the Z_2^p-periodogram at ∼2.594 39 s (see Figure 1). The probability of this peak (with a Z_2^p value of 39.66) to appear by chance in the search, taking into account the number of trials (1177), is 6 × 10^{-5}. This corresponds to a 4-sigma detection. To refine our period estimate, we used an epoch folding technique and fitted the peak in the χ^2 versus trial period distribution as described in Leahy (1987). We obtained a best period of 2.594 39 ± 0.000 04 s. The corresponding folded lightcurve is shown in Figure 1; the pulse profile is double-peaked and the root mean square pulsed fraction is (13 ± 2)% in the 2–10 keV energy range and after subtracting the background. The period derivative inferred from the Chandra and XMM-Newton measurements is (1.9 ± 0.4) × 10^{-11} s^{-1}. Assuming that the spin-down rate has remained constant at this value, we repeated the search for pulsations.
Spin-down rate of SGR 1627–41

Figure 1. $Z_2^2$-periodogram of SGR 1627–41 in the 2–10 keV energy range. The peak at 2.594 s is significant at $4\sigma$. The inset shows the corresponding pulse profile (2–10 keV, not background-subtracted).

in archival X-ray data described in [Esposito et al. (2009)]. Again, we did not detect any significant signal.

To search for possible pulse shape variations as a function of time, we compared the Chandra lightcurve with that obtained in 2008 September with XMM-Newton by using a two-dimensional Kolmogorov–Smirnov test (Peacock 1983; Fasano & Franceschini 1987). Taking into account the unknown relative phase alignment, the two profiles are compatible. In fact, the probability that they come from the same underlying distribution is about 70%.

3 SEARCH FOR RADIO PULSATIONS

The $P$–$\dot{P}$ diagram for magnetars (Figure 2) shows that the timing properties of SGR 1627–41 are remarkably similar to those of the anomalous X-ray pulsar 1E 1547.0–5408. The latter source, together with XTE J1810–197 (Camilo et al. 2006), is one of the two magnetars known to sporadically emit radio pulses (Camilo et al. 2007, 2008; Burgay et al. 2009). Although SGR 1627–41 was not detected as a radio pulsar immediately after the 2008 May activation (Camilo & Sarkissian 2008), we searched for radio emission in archival data taking advantage of the new pieces of information about its timing properties.

We analysed archival radio observations performed at 1.4 GHz with the Parkes radio telescope. The data were taken on 1999 March 22 with the central beam of the 20-cm multibeam receiver (Staveley-Smith et al. 1996) over a bandwidth of 288 MHz split in 96 3-MHz channels. The 2.3 hours observation was 1-bit sampled every 1 ms.

We folded the data with 6250 values of the period spanning ±5 ms (corresponding to a 4σ uncertainty on the value of $P$) around the nominal value $P_{PKS} = 2.5889(12)$ s extrapolated from the current best X-ray ephemeris at MJD 51259, which corresponds to the epoch of the Parkes observation. Given the position in the sky of SGR 1627–41, assuming a distance of 11 kpc (Corbel et al. 1999), and a model for the distribution of free electrons in the interstellar medium (Cordes & Lazio 2002), the expected dispersion measure is $DM \sim 1150$ pc cm$^{-3}$. Given the uncertainties in the DM determination, we chose to de-disperse the signal with 390 DM values ranging from 0 to 2300 pc cm$^{-3}$. The expected broadening of the pulse due to interstellar scattering at SGR 1627–41 position, according to the Cordes & Lazio model (Cordes & Lazio 2002), is $\sim 50$ ms at 1.4 GHz; the uncertainties of the interstellar medium model in this respect are, however, even larger than those related to the DM. The number of period and DM steps was hence chosen in such a way to produce a maximum total smearing in the folded profile of <10 ms, also compatible with the number of bins $n_{bin} = 256$ in which the folded profile was subdivided. No signal with signal-to-noise ratio greater than 6 was found in this search.

Using the radiometer equation (e.g. Manchester et al. 2001) we find an upper limit for radio pulsed emission of 0.22 mJy for an approximately sinusoidal pulse profile, and of 0.08 mJy for a duty cycle of 10%.

Since the two known radio-pulsating magnetars are sometimes visible through their individual pulses (Camilo et al. 2007), a search for single dispersed pulses has been carried out, leading to the detection of a faint (signal-to-noise ratio: 6.2) candidate signal at $DM \sim 93$ pc cm$^{-3}$. The DM of the putative pulse (to be confirmed with further observations) is however likely too small to be associated with SGR 1627–41. A blind search for periodic signals at $DM = 93$ pc cm$^{-3}$ resulted in no significant detection down to a flux density limit of $\sim 0.01$ mJy for a long period pulsar and $\sim 0.2$ mJy for a millisecond pulsar.

4 The accuracy of the timing solution does not allow us to phase-connect the XMM-Newton and Chandra data.
4 DISCUSSION AND CONCLUSIONS

With a rotation period of $2.59\,\text{s}$ (Esposito et al. 2009), SGR 1627–41 is the second fastest spinning magnetar, after 1E 1547.0–5408 ($P = 2.07\,\text{s}$; Camilo et al. 2007). Using an archival Chandra observation, we have been able to obtain a second period measurement. The Chandra and XMM-Newton datasets, separated by about 114 days, imply a long-term average spin-down rate $\dot{P} = (1.9 \pm 0.4) \times 10^{-11}\,\text{s}^{-1}$. This value is compatible with the range $1.2 \times 10^{-11}\,\text{s}^{-1} < \dot{P} < 6 \times 10^{-10}\,\text{s}^{-1}$ derived from the long XMM-Newton observation.

Within the usual vacuum dipole framework (see e.g. Lorimer & Kramer 2004), the spin-down rate can be used to infer a surface magnetic field strength of $B \approx 3.2 \times 10^{13}(P/P)^{1/2} \approx 2 \times 10^{13}\,\text{G}$, confirming the magnetar nature of SGR 1627–41. The characteristic age and the spin-down luminosity are $\tau_c = 5\,\dot{P}/P \approx 2.2\,\text{kyr}$ and $\dot{E} = 4\pi^2 I P^3\dot{P}^{-2} \approx 4 \times 10^{34}\,\text{erg}\,\text{s}^{-1}$, respectively, where $I \approx 10^{45}$ g cm$^2$ is the moment of inertia of the neutron star.

Our newly determined values of $P$ and $\dot{P}$ for SGR 1627–41 are reported in Figure 2 together with all the values available up to now for magnetar sources. As can be seen in Figure 2 where the vertical bars indicate variability ranges, magnetar spin-down rates can be highly variable. For this reason the magnetic fields, characteristic ages, and spin-down luminosities inferred for magnetars should be taken with particular caution. In particular, this applies to SGR 1627–41, for which we have no information of possible variability of the period derivative. It is interesting to note that SGRs and AXPs do not populate different regions of the $P$–$P\dot{P}$ plane, so that it would be difficult to discriminate between the two groups on the basis of their timing properties. This further supports the idea that SGRs and AXPs are actually members of the same class. What Figure 2 suggests, instead, is that transient and persistent sources might have different characteristics. The transient magnetars (in blue in Figure 2), in fact, appear to have lower magnetic fields with respect to the persistent ones (irrespective of their classification, AXPs or SGRs). In this respect the position of SGR 1627–41 in the $P$–$P\dot{P}$ diagram is similar to that of other transient magnetars. The only exceptions are 4U 0142+614 and 1E 2259+586 which are not transient but have among the lowest derived values of $B$.

The neutron-star characteristic age is consistent with an association of SGR 1627–41 with the supernova remnant (SNR) G337.0–0.1 (see Esposito et al. 2009 and references therein). At a distance of 11 kpc (Corbel et al. 1999), the observed SNR angular diameter of $\sim 1$ arcmin would correspond to a physical diameter of $\sim 9$–10 pc. This is similar to the observed sizes for other young remnants (1–3 kyr, at the beginning of the Sedov phase) hosting a neutron star, like for example Kes 73 (Gotthelf & Vasisht 1997) and RCW 103 (Carter et al. 1997).

The spin-down luminosity of SGR 1627–41 is one of the highest among magnetars and is roughly equal to the Chandra luminosity of $3 \times 10^{34}\,\text{erg}\,\text{s}^{-1}$ (Esposito et al. 2009). In magnetars $\dot{E}$ ranges, in fact, from $6 \times 10^{31}\,\text{erg}\,\text{s}^{-1}$ for 1E 2259+586 (Gavriil & Kaspi 2005) to $10^{34}\,\text{erg}\,\text{s}^{-1}$ for 1E 1547.0–5408 (Camilo et al. 2007). The observed correlation between the spin-down power and the nonthermal X-ray emission for ordinary pulsars by Possenti et al. (2002) predicts for SGR 1627–41 an $X$-ray luminosity of $5 \times 10^{33}\,\text{erg}\,\text{s}^{-1}$ and a maximum value $L_{X,\text{crit}} = 10^{18.85}(\text{erg}\,\text{s}^{-1})^{1/4} \approx 5 \times 10^{32}\,\text{erg}\,\text{s}^{-1}$. This makes it implausible that SGR 1627–41 is powered by star rotation unless the conversion efficiency is extremely high. Moreover, Camilo et al. (2007) noted in the case of 1E 1547.0–5408 that, despite the fact that the spin-down luminosity is comparable with the X-ray luminosity, it is unlikely that a significant fraction of the X-ray emission is powered by rotation, since the source displays the distinctive features of the pulsars powered by magnetic field decay. In fact, at variance with rotation-powered pulsars and cooling neutron stars, the source showed flux variations by orders of magnitude. Furthermore, the X-ray spectrum of 1E 1547.0–5408 includes a thermal component which is hotter ($kT \approx 0.4\,\text{keV}$) than that expected from a young, cooling neutron star (see for example Yakovlev et al. 2002). Such high temperatures are unusual among magnetars, the surface of which can be substantially heated by energy deposition following burst-active periods and/or by dissipative currents in the crust. The considerations by Camilo et al. (2007) also apply also to SGR 1627–41, with its X-ray luminosity variable by a factor of $\sim 100$ (between the historical minimum and maximum, $\sim 2 \times 10^{35}\,\text{erg}\,\text{s}^{-1}$ and $\sim 3 \times 10^{35}\,\text{erg}\,\text{s}^{-1}$; Esposito et al. 2008). The only high-statistics spectrum of SGR 1627–41, collected by XMM-Newton in 2008 September, when the luminosity was still high ($\sim 10^{34}\,\text{erg}\,\text{s}^{-1}$), suggests the presence of a thermal component, a blackbody with temperature $kT \approx 0.5\,\text{keV}$ (Esposito et al. 2009). Finally, we also note that it is unlikely that the low luminosity observed in SGR 1627–41 while it was approaching its historical minimum during its decade-long quiescence arose mainly from rotational power. The X-ray emission was in fact very soft and possibly thermal (Kouveliotou et al. 2003; Mereshetti et al. 2006).

The mechanisms behind the pulsed radio emission of magnetars are poorly understood. It is not ruled out that their radio emission is related to the braking in a way similar to that of the ordinary radio pulsars, but the radio properties of the two magnetars detected so far in radio, XTE J1810–197 and 1E 1547.0–5408, are quite distinguishing: their flux is highly variable on daily timescales, their spectrum is very flat, and their average pulse profile changes with time, from minutes to days (Camilo et al. 2006, 2007, 2008; Kramer et al. 2007). Remarkably, XTE J1810–197 and 1E 1547.0–5408 share small periods and high spin-down luminosities. Thus, in view of the similarities with the two radio-pulsating magnetars, SGR 1627–41 is a good candidate to be searched for pulsars at radio frequencies.

Our analysis of archival Parkes data obtained at 1.4 GHz in 1999 March (about 9 months after the first detected X-ray outburst of SGR 1627–41) showed no pulsed signal in a $\pm 4\sigma$ interval bracketing the expected period, down to a flux density limit of $S \approx 0.08$ mJy for a pulsar with a 10% duty cycle (twice as better a limit than what obtained by Camilo & Sarkissian (2008) with observations following the 2008 outburst). For a distance of $d = 11$ kpc (Corbel et al. 1999), this limit translates into a pseudo-luminosity $L = 8\pi^2$ of approximately 10 mJy kpc$^2$, significantly smaller than the 1.4 GHz luminosity of the two known radio magnetars at their peak ($\sim 100$–200 mJy kpc$^2$), although still much larger than the smallest known luminosity of ordinary young (with spin-down age $\tau_c < 10^7$ yr) pulsars ($\sim 1$ mJy kpc$^2$). Given the remarkable and rapid variability of the pulsed flux shown by the two aforementioned known radio magnetars, the negative results of the two searches performed so far on SGR 1627–41 (Camilo & Sarkissian 2008).

5 With the notable exception of the young pulsar PSR J1846–0258 at the centre of the supernova remnant Kes 75, which showed large flux and spectral variations (Gavriil et al. 2008). This source, however, shares some (but not all) characteristics of magnetars, including a (relatively) high dipole magnetic field of $5 \times 10^{13}\,\text{G}$ and the emission of SGR-like short bursts (Gavriil et al. 2008), and it is therefore unclear whether it is purely rotation-powered.
and this work) cannot anyway be conclusive and a longer term monitoring is necessary for satisfactorily assessing the radio properties of this source.

ACKNOWLEDGMENTS

This research has made use of data obtained from the Chandra Data Archive and software provided by the Chandra X-ray Center (CXC) in the application package CIAO. The Parkes radio telescope is part of the Australia Telescope which is funded by the Commonwealth of Australia for operation as a National Facility managed by CSIRO. The authors thank the referee, Vicky Kaspi, for her constructive comments. The Italian authors acknowledge the partial support from ASI (ASI/INAF contracts I/088/06/0 and AAE TH-058). SZ acknowledges support from STFC. FM and DG acknowledge the CNES for financial support. NR is supported by an NWO Veni Fellowship.

REFERENCES

Camilo F., Sarkissian J. 2008, Astron. Tel., 1558
Woods P. M., Kouveliotou C., Gögüş E., Hurley K., Tomskick J. 2008, Astron. Tel., 1564

This paper has been typeset from a TeX/LATEX file prepared by the author.