Abstract—Slag fuming is a process of extracting zinc from molten slag in the form of metal vapor by injecting or adding a reducing source such as pulverized or lump coal, natural gas, etc. Top Submerged Lance (TSL) technology has been successfully applied to extract zinc by a fuming process from residues from the zinc industry, ISF and QSL slag and Lead blast furnace slag. A Computational Fluid Dynamic model has been developed for zinc slag fuming process from ISF slag to investigate details of fluid flow and heat transfer in the furnace. The models integrate complex combustion phenomena and chemical reactions with the heat, mass and momentum interfacial interaction between the phases present in the system. The model is based on 3-D Eulerian multiphase flow approach and it predicted the velocity and temperature field of the molten slag bath and side wall heat fluxes. The model also predicted the mass fractions of slag and gaseous components inside the furnace. The model confirmed that rate of zinc fuming increases with temperature and is broadly consistent with experimental data.

Index Terms—Slag fuming, CFD, Top Submerged Lance, Zinc, Multiphase.

I. INTRODUCTION

Primary production of zinc and lead produces slag or residues, which can contain significant amounts of zinc. The zinc content in these depends largely on the type of concentrate and residue materials, method of extraction and equipment used. Slag fuming is basically a secondary operation which is an important unit operation in the extraction of non-ferrous metals. Slag fuming has been used since 1930s to recover zinc from lead blast furnace slag [1]. It is mostly a batch process, in which a reducing mixture of air and pulverized coal is injected into the molten slag together with lump coal, however, Korea Zinc also fume in continuously operating furnaces. The coal-air mixture reduces the zinc oxide from the slag to metallic zinc vapor.

Zinc Fuming

Suzuki et al. [5] investigated the factors effecting the zinc fuming kinetics such as gas or slag composition, gas blow rate, slag temperature, viscosity and surface tension on a crucible scale experimental work. In their research, Suzuki et al. [5] found that formation of bubbles in the molten slag bath has a great influence on the zinc fuming kinetics. Richards et al. [2-4] carried out extensive research on kinetics of zinc slag-fuming process. In the first part of their research [2], they used industrial measurements to investigate the kinetic

II. LITERATURE REVIEW

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phenomena in the zinc slag-fuming process. The industrial work consisted of slag sampling through the cycles of different fuming operations. They reported that the zinc reduction curve is linear with time and a portion of the injected coal entrains in the slag.

Later, Richards and Brimacombe [4] developed a mathematical model of zinc slag fuming based on two reaction zones; (i) an oxidizing zone in the tuyere gas stream and a separate (ii) reduction zone at the gas slag interface. The authors reported that about 33% of the injected coal was entrained in the slag, 55% combusted in the tuyere gas column and 12% bypassed the bath completely. Richards and Brimacombe [3] elucidated the rate limiting steps of the fuming process and predicted the influence of process variables on fuming by using the two zone kinetic model [4]. The model predicts that fuming efficiency reaches maximum with increasing residence time of coal particles in the slag.

Cockcroft et al. [6] subsequently improved the model of Richards et al. [3] by further consideration of mass transfer, chemical kinetics and heat transfer in the system and also including the behavior of lead in the bath. Cockcroft et al. [7] reported that high pressure coal injection increased coal entrainment about 25%, from 65% for low pressure to 90% for high pressure. As a result fuming rates were increased substantially, to between 70% and 90%, depending on the charge mix. Richards [8] commented that coal entrainment is controlled by injection conditions whereas bath temperature is a function of coal combustion and ferrous oxide oxidation.

Further industrial studies have followed the studies by Richards et al. [2-4, 8, 9] and Cockcroft et al. [6, 7]. Miyake [10] described different aspects and optimized plant operating conditions of a slag fumer at the Hachinohe Smelter. Choi and Lee [11], Sofra et al. [12], Hughes et al. [13], Hoang et al. [14] described the Ausmelt’s Top Submerged Lance (TSL) technology for the processing of secondary zinc feed materials, including zinc plant leach residues and EAF dust. More recently, the present authors [15] developed a CFD model for top submerged lance gas injection process, which they validated against an air-water system.

Although commercial slag fuming is well established, there have only been a few numerical modeling studies on zinc fuming kinetics. Kellogg [16] developed the first computer model for slag fuming process using programming language Fortran IV. In that model, Kellogg assumes stepwise equilibrium during each micro-step (0.1 minute in a 90 minute period). No CFD analysis has been found in the open literature regarding slag fuming. In this paper, we describe a model we have developed that includes combustion, reactions kinetics in CFD.

III. COMPUTATIONAL PROCEDURE

A 3D model of the Ausmelt pilot plant was developed using CAD. A schematic diagram of the model is shown in Fig. 2(a). The modeled furnace has a diameter of $D = 0.5$ m and length $Z = 1.68$ m. The modeled furnace was filled up to $L = 0.6$ m with ISF slag of composition shown by point A in Fig. 3. A vertical lance with an annulus of inner diameter $d_i = 30$ mm and outer diameter $d_o \approx 42$ mm was fitted at the centre of the furnace. Air was injected through the annulus of the lance and CH$_4$ as fuel through the central hole into the slag bath. Necessary heat in the bath for smelting and reduction of the slag is supplied by combusting CH$_4$ at the lance tip.

A schematic diagram of the modeled furnace is shown on Fig. 2(a). Generated 3D course grid is shown in Fig. 2(b), fine grid is not shown here for visual clarity. The computational grid (283344 cells) used in the present study is too dense for visual presentation. All the cells in the calculation domain were polyhedral with a large number of hexahedral cells. As the computational domain consisted of hybrid unstructured meshes in curvilinear non-orthogonal coordinate system with Cartesian base vectors and refined regions in some locations, mentioning number of cells in each direction is complicated. The meshing procedure was carried out using the ANSYS Combustion module 17.1.

The multiphase flow simulation is based on Eulerian approach where gas and liquid phases interact with each other and there is significant exchange of momentum and energy between phases. In addition to mass and energy exchange between the constituents in each phase, there is also mass exchange between the gas and molten slag phase due to the phase transformation for chemical reaction in the slag bath. The model was developed by using commercial CFD package AVL FIRE 2008.2. Interfacial mass and energy exchange were modeled by using user-defined subroutines (UDF). The model developed include the following features,

1. Unsteady state multiphase solution for momentum and continuity.
2. Standard $k$-$\varepsilon$ turbulence model for the turbulence modeling.
3. A cell centered finite volume approach was used to discretise the governing equations and the resulting discretised equations were solved iteratively using segregated approach.
4. Pressure and velocity were coupled using the SIMPLE algorithm [18].
5. For momentum and turbulence, first order upwind differencing scheme was used whereas central differencing scheme with second order accuracy was used for the continuity equation
6. All boundary conditions were chosen to match the flow condition of the pilot plant trials of the Ausmelt pilot plant.

Basic Eulerian equations, describing multiphase combusting system are given by the conservation equations for continuity, momentum and energy in the gas-liquid interface is discussed below:

**Interfacial Momentum Exchange**

Momentum equation solved for the simulation can be expressed as,

\[
\frac{\partial \alpha_k \rho_k v_k}{\partial t} + \nabla \cdot (\alpha_k \rho_k v_k v_i) = -\alpha_k \nabla p + \nabla \cdot (\alpha_k \mathbf{v}_k + T_k) \\
+ \alpha_k \rho_k f + \sum_{l=1}^{N} M_{kl} + \sum_{l=1}^{N} \Gamma_{kl}
\]

(4)

\(\sum_{l=1}^{N} \Gamma_{kl}\) represents the interfacial mass exchange and \(\sum_{l=1}^{N} M_{kl}\) represents the momentum interfacial interaction between phases \(k\) and \(l\), \(f\) is the body force vector which comprises of gravity \((g)\), \(p\) is pressure. Momentum interfacial exchange between gas and liquid has been modeled by implementing interfacial momentum source at the interface which includes drag and turbulent dispersion forces [17]:

\[
M_c = C_D \frac{1}{8} \rho_c A_f v_r^2 + C_{TD} \rho_c k_c \nabla \alpha_d = -M_d
\]

(5)

where \(c\) denotes continuous and \(d\) denotes the dispersed phase. The first term in equation (5) represents mean contributions due to drag force and the second term takes into account the turbulence effect. The turbulence effect is represented by a global dispersion effect, which is proportional to the void fraction gradient (cited in [20]).

The drag coefficient, \(C_D\), is a function of the bubble Reynolds number, \(Re_b\). The following correlation for drag coefficient, \(C_D\), was used [17]:

\[
C_D = \frac{24}{Re_b^2} + 0.15 Re_b^{0.67}
\]

(6)

Bubble Reynolds number, \(Re_b\), and can be defined as:

\[
Re_b = \frac{\nu D_b}{\nu_c}
\]

(7)

Where \(\nu_c\) is the kinematic viscosity for continuous phase. Relative velocity is defined as:

\[
\mathbf{v}_r = \mathbf{v}_d - \mathbf{v}_c
\]

The interfacial area density for bubbly flow can be expressed as [17]:

\[
A^*_b = \frac{4 \pi A_r}{D_b}
\]

(8)

where \(D_b = 0.1\) mm is the bubble diameter and \(A_r\) is dispersed phase volume fraction. Bubble dispersion coefficient used in equation (5) was,

\[
C_{TD} = 0.07
\]

**Combustion Modeling at the Lance Tip**

For gas phase reaction, only one step \(\text{CH}_4\) combustion reaction at the lance tip is considered as described by (9),

\[
\text{CH}_4 + 2(2\text{O}_2 + 3.76\text{N}_2) \rightarrow \text{CO}_2 + 2\text{H}_2\text{O} + 2 \times 3.76\text{N}_2
\]

(9)

Species transport equation solved for gas phase reaction can be expressed as:

\[
\frac{\partial}{\partial t} (\rho \psi_k) + \frac{\partial}{\partial x_i} (\rho (\mathbf{v}_d - \mathbf{U}_k) \psi_k) = \frac{\partial}{\partial x_i} \left( \Gamma_{ij} \frac{\partial \psi_k}{\partial x_j} \right) + S_{\psi_k}
\]

(10)

where \(\psi_k\) represents the mass fraction of an individual chemical species \(k\). \(K_{GAS}\) is the total number of chemical species. \(\Gamma_{\psi_k}\) can be defined as:

\[
\Gamma_{\psi_k} = \left( \rho \frac{D_{k,m}}{Sc_f} + \frac{D_{k,t}}{Sc_f} \right)
\]

(11)

where \(D_{k,m} [\text{m}^2/\text{s}]\) is the diffusion coefficient for each species \(k\) in the mixture and \(Sc_f = 0.7\) is the turbulent Schmidt number. The mass source \(S_{\psi_k}\) in the species transport equation is defined as,
\[ S_{ik} = \bar{\bar{\omega}}_{ik} M_k V_{Cell} \]  

(12)

Where, \( \bar{\bar{\omega}}_{ik} [\text{kmol/(m}^3\text{s)}] \) is the reaction rate of species \( k \) and \( M_k [\text{kmol/kg}] \) is the molecular weight of species \( k \) and \( V_{cell} [\text{m}^3] \) is the volume of the computational cell. The rate of the reaction of species \( k \), \( \bar{\bar{\omega}}_{ik} [\text{kmol/(m}^3\text{s)}] \) is calculated by the Eddy Break up combustion model [21].

\[ \bar{\bar{\omega}}_{ik} = -\mathbf{P}\frac{\mathbf{F}}{n_k} \min \left[ C_{kl} C_{\alpha} \frac{Y_{ki}}{L_k} \sum_{l=1}^{N} C_{lk} C_{\alpha} \frac{Y_{kl}}{L_k} \right] \]  

(13)

**Interfacial Energy Exchange:**

Total enthalpy conservation equation solved for the model can be expressed as,

\[ \frac{\partial q_{ik}}{\partial t} + \nabla \cdot \left( \nabla h_k + q_{ik} \right) = -\nabla \cdot \left( \mu_k \nabla h_k \right) + \nabla \cdot \left( \rho_k \alpha_k \nabla \theta_k \right) \]  

(14)

where \( q_{ik} \) is the enthalpy volumetric source, \( h_k \) is defined as,

\[ q_{ik} = k_{ik} \frac{\partial h_k}{\partial \alpha_k} \]  

(15)

where \( k_{ik} \) is the phase \( k \) thermal conductivity, \( h_k \) is the phase \( k \) enthalpy. Turbulent heat flux, \( q_{ik}^t \), equals:

\[ q_{ik}^t = \frac{\mu_{ik}}{\sigma_{ik}} \frac{\partial h_k}{\partial \alpha_k} \]  

(16)

\[ \Gamma_{kl} \text{ and } H_{kl} \text{ in equation (14) represents mass and energy interfacial exchange between phases } k \text{ and } l. \text{ Heat generated due to the CH}_4 \text{ combustion at the lance tip is transferred to the molten slag phase by considering interfacial energy exchange at the gas-liquid interface. Heat transfer between the two phases is modeled by using Ranz-Marshall enthalpy exchange model [17] as follows:} \]

\[ H_k = \frac{k_k}{D_b} Nu \alpha \left( T_{cell} - T_i \right) \]  

(17)

where, \( k \) is the thermal conductivity of the molten slag phase, \( D_b \) is the bubble diameter and \( A^* \) is the interfacial area density defined as:

\[ Nu = 2 + 0.6 \frac{Re_{bb}^{0.7}}{Pr} \]  

(18)

where, \( Re_{bb} \) is the local bubble Reynolds number, and \( Pr \) is the Prandtl number.

**Interfacial Mass Exchange**

Interfacial mass exchange at the gas-liquid interface in the slag fuming process occur only due to the chemical reaction in the slag phase. Chemical species in the slag phase has been defined by a number of scalars and the following scalar equation has been solved for each scalar for slag phase reaction.

\[ \frac{\partial}{\partial t} \alpha_i \rho_i \phi_i + \nabla \cdot (\alpha_i \rho_i \nabla \phi_i) = \nabla \cdot (\alpha_i \rho_i \mathbf{D}_i \nabla \phi_i) + \mathbf{S}_i \]  

(19)

where \( S_{ki} \) is the source term for different scalars.

Phase transformation between molten slag and gas phase was considered by the following equation [17],

\[ \Gamma_v = C_m \alpha_s \alpha_d \rho_s \]  

(20)

Where, \( c \) and \( d \) denotes the continuous and disperse phase, \( C_m \) is the rate of phase transformation, \( \rho_s \) is the density for continuous phase, \( \alpha \) is the volume fraction and volume fraction exponent used in the model are \( n_1 = 1 \) and \( n_2 = 0 \).

**Fluid properties and initial condition**

The flow was started with small initial values assigned to \( k \) and \( c \), which made the initial turbulent viscosity roughly equal to the kinematic viscosity for molten slag. For gas phase reaction given in equation (9), fluid and thermal properties of the different species involved in the solution process (density, specific heat, dynamic viscosity, molecular weight, thermal conductivity, diffusion coefficient) has been considered from the internal thermodynamic database of AVL FIRE [22]. The fluid and thermal properties for molten slag phase are mentioned in Table I.

### Table I: Fluid and thermal properties of molten slag phase

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Density (kg/m³)</td>
<td>3500</td>
</tr>
<tr>
<td>Specific heat (J/kg K)</td>
<td>400</td>
</tr>
<tr>
<td>Dynamic viscosity (Ns⁻¹m⁻²)</td>
<td>0.015</td>
</tr>
<tr>
<td>Thermal conductivity (W/m K)</td>
<td>10</td>
</tr>
<tr>
<td>Turbulent Prandtl number</td>
<td>0.5</td>
</tr>
<tr>
<td>Reference pressure (Pa)</td>
<td>100000</td>
</tr>
<tr>
<td>Reference temperature (K)</td>
<td>1500</td>
</tr>
</tbody>
</table>

Typical turbulence quantities at the inlet of the domain were calculated from inlet velocities by considering turbulence intensity \( I = 0.05 \) where, \( I = u'/U_{inlet} \equiv 0.16(Re)^{1/8} \).

**IV. RESULTS AND DISCUSSIONS**

Zinc fuming is a very complex process to simulate and it is necessary to make a number of assumptions to simplify the simulation. A large number of complex reactions are involved, such as: reduction of zinc oxide and ferric iron, fuel combustion, oxidation of ferrous iron oxide. In the present simulation, only reduction of zinc oxide and fuel combustion has been considered. We ignore the other reactions taking place in the system (the oxidation of Fe is likely to be important). Also, carbon was considered as a separate species assuming that 100% of the coal is fixed carbon with no volatile and ash content (which we know to be incorrect). As the numerical simulation is based on Eulerian approach, it doesn’t show the exact plume shape with sharp gas-liquid interface (e.g. collapsing bubble plumes). However, the results here represent a significant step in developing a comprehensive model.

Temperature distribution for two separate phases is shown in Fig. 4. Fig. 4(a) shows the predicted temperature profile of the molten slag phase only after 30 seconds of the reduction stage. Because of the computational limitation, the simulation was run only for 30 seconds of real time. The present simulation only considers the reduction stage of the zinc fuming process. The simulation results revealed that there is
non-uniform temperature distribution in the molten slag bath. This temperature profile doesn’t imply steady state distribution. These non-uniform temperature distributions in the slag bath are expected to be uniform with longer simulation time.

From the simulation results, the molten slag bath can be divided into three zones: combustion zone near the lance tip (1680-1780 K), bath zone below the lance tip in the bath (1500-1600 K) and the bottom zone near the bottom surface of the furnace (1380-1430 K). Near the surface area of the molten slag bath, there was a thin layer of gas-liquid mixture. The transport properties of the molten slag phase influences this temperature distribution in the slag and the concentration of FeO (which we currently ignored) is likely to influence these properties significantly. Fig. 4(b) shows the temperature distribution for gaseous phase inside the furnace which shows the highest temperature distribution is at the lance tip and above the bath. Fig. 5 shows the volume fraction distribution for molten slag phase after 25 seconds of transient simulation. The sloshing and splashing phenomena above the slag bath is clearly visible from the volume fraction plot.

After the initiation of the combustion at the lance tip, the plume becomes larger because of the combustion and expansion of the gases in the slag bath. There is massive agitation in the slag bath and sloshing phenomena is observed from the simulation. The CFD software we used (AVL FIRE) enables us to capture results even for micro second. The simulation results predict that zinc fuming initiates from the near the surface area of the molten slag bath in the combustion zone where CO\(_2\) forms as a product of combustion of CH\(_4\). In the combustion zone, CO forms from the CO\(_2\) by Boudouard reaction as mentioned in equation (2). CO thus formed initiates the first fuming process in the bath. Fig. 6(a) shows the initial stage zinc fuming process near the lance tip area. The fuming process accelerates from the bath near the surface area where the temperature rises rapidly and carbon reacts directly with ZnO in the molten slag. Fig. 6(b) shows the fumed zinc distribution inside the furnace from the molten slag bath.

Fig. 7(a) shows the species mass fraction distribution of CH\(_4\) in the combustion chamber at the lance tip after 10.5 seconds of the simulation which shows CH\(_4\) being almost combusted because of stoichiometric combustion. Because of the swirling effect in the annular region of the lance, O\(_2\) in the air mixes well with the CH\(_4\) in the combustion chamber and ensures fuel-efficient combustion at the lance tip. Formation of CO\(_2\) in the bath is shown in Fig. 7(b). The present simulation was carried out on the assumption that the CO/CO\(_2\) ratio is 1.
Fig. 8 shows the fuming rate of Zn from the bath as a function of temperature, experimental data are also shown for comparison. Experimental work was done by Waladan et. al [23] on crucible scale test work with ISF slag of 9.6% ZnO. The present simulation was carried out by considering ISF slag of 18% ZnO shown by point A in Fig. 3. Minor elements in the ISF slag were not taken into consideration for the present simulation. The produced curve shows the increasing fuming rate with temperature, which is also consistent with experimental results.

The simulation results showed zinc concentration in the slag decrease linearly with time. The linear time dependence of the zinc elimination rate reveals the zero order reaction kinetics, which is also consistent with the experimental results of Richards et. al [2]. Few improvement of the model, particularly, the treatment of the oxidation of Fe and providing a more realistic treatment of the behavior of coal will be incorporated. Even with these problems, these results appear very promising.

V. CONCLUSIONS

The simulation results give some interesting insights for complex metallurgical flows and transient concentrations of slag components and gaseous species inside the molten slag bath. These simulations reveal the zero order reaction kinetics of the zinc fuming process and suggest temperature distribution and plume shape in the molten slag bath for the 30 seconds of simulation. The results also showed that zinc elimination rate increases with temperature. The model is still in the improvement and validation phase. Detail reaction kinetics with all the elements of ISF slag will be incorporated to improve the model in addition to longer simulations. This model forms the basis in developing more complex models to help predict actual operations beyond simple flow modeling.

ACKNOWLEDGMENT

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