Molecular simulation of the shear viscosity and the self-diffusion coefficient of mercury along the vapor-liquid coexistence curve

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In earlier work [G. Raabe and R. J. Sadus, J. Chem. Phys. 119, 6691 (2003)] we reported that the combination of an accurate two-body \textit{ab initio} potential with an empirically determined multibody contribution enables the prediction of the phase coexistence properties, the heats of vaporization, and the pair distribution functions of mercury with reasonable accuracy. In this work we present molecular dynamics simulation results for the shear viscosity and self-diffusion coefficient of mercury along the vapor-liquid coexistence curve using our empirical effective potential. The comparison with experiment and calculations based on a modified Enskog theory shows that our multibody contribution yields reliable predictions of the self-diffusion coefficient at all densities. Good results are also obtained for the shear viscosity of mercury at low to moderate densities. Increasing deviations between the simulation and experimental viscosity data at high densities suggest that not only a temperature-dependent but also a density-dependent multibody contribution is necessary to account for the effect of intermolecular interactions in liquid metals. An analysis of our simulation data near the critical point yields a critical exponent of $\beta=0.39$, which is identical to the value obtained from the analysis of the experimental saturation densities. © 2005 American Institute of Physics. [DOI: 10.1063/1.1955530]

I. INTRODUCTION

Recently, molecular simulation has been successfully used to predict the phase behavior of mercury. The occurrence of considerable changes in the physical properties of mercury, such as metal-nonmetal transitions, together with a high critical temperature and high toxicity, means that mercury and other liquid metals are challenging systems to investigate experimentally. For these systems, molecular simulation could have a valuable role in supplementing experimental data. However, the accuracy of predictions by molecular simulation strongly depends on the intermolecular potential involved, and the determination of a suitable potential for mercury has also proved to be a considerable challenge.

The earliest intermolecular potentials published for mercury were $(n,m)$ Lennard-Jones potentials fitted to experimental data for gas viscosities or the second virial coefficient. These potentials suffer from the inaccuracy of the underlying experimental data and are often only explicitly formulated for the calculation of specific properties. In recent years, several \textit{ab initio} studies of the potential-energy curve of the mercury dimer have been published. The \textit{ab initio} intermolecular potential reported by Schwerdtfeger \textit{et al.} can be regarded as the most accurate representation of the two-body potential-energy curve because it is in good agreement with the most recent and most accurate experimental spectroscopic data. However, it fails to predict the coexisting vapor and liquid densities and the equilibrium pressure of mercury.

The fact that simulations using an accurate \textit{ab initio} pair potential yield very poor agreement with experiment suggests that the thermophysical properties of mercury are influenced by strongly correlating multibody effects. As higher-body potentials for mercury are not available and including such contributions in a molecular simulation would be computationally prohibitive, we added an effective many-body term to the pair potential of Schwerdtfeger \textit{et al.} Using this multibody contribution, we were able to predict mercury’s phase coexistence properties, the heats of vaporization, and the pair distribution functions of mercury with reasonable accuracy.

The aim of this work is to determine whether or not the \textit{ab initio} potential by Schwerdtfeger \textit{et al.} in combination with our empirical multibody contribution can be used to accurately determine the shear viscosity and the self-diffusion coefficient of mercury.

II. THEORY

A. Effective multibody intermolecular potential

The latest attempt by Schwerdtfeger \textit{et al.} to determine an accurate intermolecular potential for mercury involved \textit{ab initio} calculations and the addition of a spin-orbital contribution, resulting in a two-body potential-energy curve given by
\[ u_2(S) = \lambda_F \sum_{j=3}^{9} a_2(\lambda, r)^{-2j} - 45.772 \times 54r^{-4.269} \times \exp(-0.672 64r). \]  
(1)

For this potential, the minimum depth is \( \varepsilon/k = 525.15 \) K and the characteristic distance parameter is \( \sigma = 3.14 \) Å. The meaning and values of the parameters in Eq. (1) can be taken from Schwertfeger et al.\(^1\)

Although this potential can be regarded as the most accurate treatment of the two-body potential-energy curve, it fails to yield reasonable results for the coexisting vapor and liquid densities and the equilibrium pressure of mercury. Therefore, it is reasonable to infer that higher-body effects may be required to adequately describe the phase behavior of mercury. In our preceding work,\(^1\) we proposed that an improvement could be achieved by including the nonadditive contributions of multibody effects into the Schwertfeger \textit{ab initio} pair potential via an effective \( C_9/r^9 \) term. The result was a semiempirical effective potential given by

\[ u_n = u_2(S) + \frac{C_9}{r^9} \]  
(2)

with \( C_9 \) and \( r \) in Eq. (2) expressed in terms of a.u.

We previously\(^1\) performed Monte Carlo Gibbs-ensemble simulations for vapor-liquid equilibria (VLE) at different temperatures to determine the values of \( C_9 \) required for good agreement with experimental liquid phase densities. We observed\(^1\) a linear dependency for the \( C_9 \) values with respect to temperature and were able to accurately fit these values to a simple linear function of \( kT/\varepsilon \):

\[ C_9 = -16 020.46 - 2823.42 \left( \frac{kT}{\varepsilon} \right). \]  
(3)

It should be emphasized that no attempt was made in this work to specifically adjust the parameters of Eq. (3) to optimize the agreement for transport properties. Therefore, the simulation results for the shear viscosity and the self-diffusion coefficient reported here are genuine predictions.

### B. Simulation Details

The simulations were performed in an \( NVT \) ensemble of \( N \approx 500 \) particles. The volume of the simulation box was chosen in such a way that the resulting density corresponded to either the density of the liquid or the vapor phase of the vapor-liquid equilibria (VLE) at the given temperature. Information on the densities of the VLE was taken from the simulation results of our previous work\(^1\) or from experiment.\(^12\) The Gear predictor-corrector scheme\(^13\) was used to integrate the equations of motion, with a reduced time step of \( \Delta t = 0.001 \) for the liquid and dense vapor state points near the critical point, and \( \Delta t = 0.002 \) for vapor state points at low densities. The Gaussian thermostat\(^13\) was used to constrain the kinetic temperature.

The shear viscosity was determined by the Green-Kubo\(^13,14\) method of integrating the autocorrelation function of the off-diagonal elements of the viscous pressure tensor \( P_{\alpha\beta} \) given by

\[
P_{\alpha\beta} = \left\langle \frac{1}{V} \left( \sum_i P_{\alpha\beta}^{i\alpha} + \sum_i \sum_{j>i} r_{ij} F_{ij\alpha\beta} \right) \right\rangle.
\]  
(4)

where \( P_{\alpha\beta} \) and \( r_{ij} \) are the \( \alpha \) and \( \beta \) components of the momentum of particle \( i \), \( F_{ij\alpha\beta} \) is the \( \alpha \) component of the distance between the particles \( i \) and \( j \), and \( F_{ij\alpha\beta} \) is the \( \beta \) component of the force of their interaction. To improve the statistics, we averaged the autocorrelation functions over all independent off-diagonal tensor elements, resulting in

\[
\eta = \frac{V}{3kT} \int_0^\infty \left[ \langle P_{xy}(0) P_{xy}(t) \rangle - \langle P_{xy}(0) \rangle \langle P_{xy}(t) \rangle \right] dt.
\]  
(5)

The self-diffusion coefficient \( D \) was determined from the Einstein relation\(^13,14\) as the mean-square displacement along the unfolded trajectory of a tracer particle

\[
D = \lim_{t \to \infty} \frac{\langle (\mathbf{r}(t) - \mathbf{r}(0))^2 \rangle}{6t}.
\]  
(6)

As the diffusion coefficient is a single-particle property, we averaged it over all particles to improve the statistics.

The cutoff distance was set to half the box length, and the long-range corrections\(^13,14\) to the potential energy and the pressure tensor were applied. We assumed the spin-orbital contribution to the potential of Schwertfeger \textit{et al.}\(^1\) to be negligible at long distances.\(^1\)

To determine the long-range correction for the shear viscosity, we made use of the relationship between the viscosity and the finite-frequency shear modulus at zero wave vector \( G_s(0) \) (Ref. 15)

\[
\eta = \tau \cdot G_s(0)
\]  
(7)

with \( \tau \) being the Maxwell relaxation time. Following Zwanzig and Mountain,\(^16\) \( G_s(0) \) can be determined from the intermolecular potential \( u(r) \) by

\[
G_s(0) = \nu kT + \frac{2\pi}{15} \int_0^\infty dr \, g(r) \frac{d}{dr} r^4 \frac{d u}{dr}
\]  
(8)

Thus, by assuming that the pair distribution function \( g(r) \) = 1 for \( r > r_{\text{cut}} \) its long-range correction becomes

\[
G^{\text{LRC}}_s(0) = \frac{2\pi}{15} \int_{r_{\text{cut}}}^\infty dr \, \frac{d}{dr} r^4 \frac{d u}{dr}.
\]  
(9)

To calculate the long-range correction of the shear viscosity by

\[
\eta^{\text{LRC}} = \tau \cdot G^{\text{LRC}}_s(0),
\]  
(10)

we need to determine the relaxation time \( \tau \). This is done through its definition given by Eq. (7), using the short-range results for viscosity from the Green-Kubo formulation and the short-range value of \( G_s(0) \) calculated from Eq. (8) with the upper limit of integration set to \( r_{\text{cut}} \). This integral can be evaluated numerically or by making use of the fact that for every property \( \langle A \rangle \) in a system of \( N \) particles there is another
The experimental data for shear viscosity are mainly re-

A comparison with the expression in Eq. (2) is easy to evaluate during the simulation. After a summation over all pairs within \( r_{\text{cut}} \), adding the ideal part, we get the short-range value of \( G_\infty(0) \). As the long-range corrections remain constant throughout the simulation, we determined the Maxwell relaxation time at the end of a run from the ensemble average of the short-range values of \( G_\infty(0) \) and the Green-Kubo viscosity, and added the long-range correction \( \eta^{\text{LRG}} \) given by Eq. (11) afterwards. We found that the long-range correction for the viscosity was smaller than the uncertainties of the short-range viscosity values.

For every state point an equilibration phase of 2 000 000 time steps preceded the actual simulation to relax the system to thermodynamic equilibrium for a given temperature and density. A production run consisted of 2 000 000 time steps for a liquid or dense vapor phase point, and up to 8 000 000 time steps for vapor state points at low densities. During a production run for a liquid or a dense gas point, the off-diagonal elements of the viscous pressure tensor and the mean-square displacement of all particles were stored every tenth time step, and 100 stored values were used to determine the autocorrelation function for the Green-Kubo viscosities. For every single simulation, a graphical inspection of the integral was made to check for a sufficient integration time, i.e., the decay of the autocorrelation function to zero during this time. In the case of low vapor densities, the autocorrelation functions of the pressure tensor elements decay very slowly, resulting in the long simulation runs as mentioned above. The interval of data storage had to be increased to 20 time steps, and 1000–2000 stored values had to be used to determine the integral of the pressure autocorrelation function.

For every state point, ten of the above-described production runs were performed to average the equilibrium properties by using the standard block average technique. Due to the enormous computational effort for simulations at state points in the low-density range, only a few were included.

### III. RESULTS AND DISCUSSION

Our simulation results for shear viscosity in the coexisting liquid and vapor phases of mercury are given in Table I. They are compared with experimental results (77–21) in Fig. 1. The experimental data for shear viscosity are mainly restricted to temperatures below 900 K. Only a few experimental results (77–21) are available at higher temperatures and these data are inconsistent with each other. In addition to the experimental investigation of the shear viscosities, Tippelkirch et al. (21) also used an empirical modification of the Enskog theory that employs the experimental data of the VLE to calculate the shear viscosity curve of mercury along the whole coexistence line. As they found their calculation to be in reasonable agreement with experiment, it provides a useful comparison with our simulation results for the temperature range above 900 K up to the critical point at \( T_C = 1751.15 \) K.

The Chapman-Enskog (77, 22) solution of the Boltzmann equation yields the shear viscosity \( \eta_0 \) of a dilute gas

<table>
<thead>
<tr>
<th>( T ) (K)</th>
<th>( \eta^L ) (10⁻⁴ Pa s)</th>
<th>( \eta^V ) (10⁻⁴ Pa s)</th>
<th>( D^L ) (10⁻² m²/s)</th>
<th>( D^V ) (10⁻⁷ m²/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>669.17</td>
<td>15.108±1.104</td>
<td>0.0295±0.0024</td>
<td></td>
<td></td>
</tr>
<tr>
<td>766.89</td>
<td>12.645±0.818</td>
<td>0.0398±0.0026</td>
<td></td>
<td></td>
</tr>
<tr>
<td>827.26</td>
<td>11.460±0.613</td>
<td>0.0461±0.0036</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1050.30</td>
<td>8.742±0.580</td>
<td>0.0575±0.0058</td>
<td>5.9314±0.4245</td>
<td></td>
</tr>
<tr>
<td>1155.33</td>
<td>7.841±0.678</td>
<td>0.0913±0.0086</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1260.36</td>
<td>7.335±0.559</td>
<td>0.1078±0.0073</td>
<td>3.0773±0.3096</td>
<td></td>
</tr>
<tr>
<td>1365.39</td>
<td>6.769±0.424</td>
<td>0.1253±0.0126</td>
<td>2.3046±0.1786</td>
<td></td>
</tr>
<tr>
<td>1470.42</td>
<td>6.235±0.484</td>
<td>0.1475±0.0117</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1573.15</td>
<td>1.948±0.167</td>
<td>0.9751±0.0812</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1575.45</td>
<td>5.418±0.343</td>
<td>0.1815±0.0132</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1663.15</td>
<td>5.400±0.369</td>
<td>0.1954±0.0130</td>
<td>0.704±0.0620</td>
<td></td>
</tr>
<tr>
<td>1728.15</td>
<td>4.215±0.254</td>
<td>2.660±0.198</td>
<td>0.2755±0.0228</td>
<td>0.5376±0.0340</td>
</tr>
<tr>
<td>1748.15</td>
<td>3.662±0.243</td>
<td>2.945±0.238</td>
<td>0.3452±0.0297</td>
<td>0.4585±0.0272</td>
</tr>
<tr>
<td>1749.15</td>
<td>3.602±0.208</td>
<td>2.963±0.248</td>
<td>0.3455±0.0254</td>
<td>0.4449±0.0346</td>
</tr>
<tr>
<td>1750.15</td>
<td>3.523±0.203</td>
<td>3.086±0.215</td>
<td>0.3455±0.0254</td>
<td>0.4449±0.0346</td>
</tr>
<tr>
<td>1751.15</td>
<td>3.200±0.221</td>
<td>0.3911±0.0328</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

FIG. 1. The comparison of experimental shear viscosity data (Refs. 77–21) for mercury along the saturation line with molecular-dynamics results obtained in this work by using Eq. (2) (III) and the ab initio potential from Schwedtfeiger et al. (Ref. 11) (A). Also shown are the results (–) for the calculation of the shear viscosity based on the empirical modification of the Enskog theory from Eqs. (14)–(20).
\[ \eta_0 = \frac{5}{16} \sqrt{\pi m k T (\pi \sigma^2 \Omega^{(2,2)})^{-1}} \]  
with \( m \) being the mass of a molecule. Tippelkirch et al. \(^{21}\) interpreted the product of the characteristic length \( \sigma \) and the collision integral \( \Omega^{(2,2)} \) as a measure of an effective cross section

\[ \sigma^2 \Omega^{(2,2)} = \sigma_{\text{eff}}^2 \]  
and determined a simple temperature dependence of \( \sigma_{\text{eff}} \) for the vapor phase

\[ \sigma_{\text{eff}}^V = 4.93 \, \text{Å} \left( \frac{234 \, \text{K}}{T} \right)^{0.285} \]  
with the melting temperature of mercury \( T_m = 234 \, \text{K} \) as a reference. The shear viscosity of the dense gas is then given by the Enskog equation

\[ \eta_v = \eta_0 \left( \frac{b_v}{v} \right) \left( \frac{\chi b_v}{v} \right)^{-1} + 0.800 + 0.761 \left( \frac{\chi b_v}{v} \right) \]  
The quantity \( b \) is the second virial coefficient of a hard-sphere fluid given by

\[ b = \frac{2 \pi}{3} N_A \sigma_{\text{eff}}^2, \]  
where \( N_A \) is the Avogadro constant, and \( v \) is the molar volume. The superscript \( V \) indicates the values of the vapor phase. The Enskog high-density correction \( \chi \) as a function of the molar volume can be taken from Alder and co-workers. \(^{24,25}\) For a given temperature, the effective hard-sphere diameter in the vapor phase is determined from Eq. \(14\) to derive the values of the second virial coefficient \( b \) from Eq. \(18\) and the reference shear viscosity \( \eta_0 \) from Eq. \(14\). Inserting the corresponding molar volume of the vapor phase \( v(T) \) from the experimental VLE data, \(^{12,17,26–28}\) and \( \chi \) from Alder and co-workers \(^{24,25}\) yields the shear viscosity of the vapor phase along the saturation line.

The Enskog theory cannot be directly employed for the calculation of shear viscosities at liquid densities because it assumes that the autocorrelation functions decay exponentially. This assumption is not valid at high densities, but Alder and co-workers \(^{24,25}\) were also able to describe the deviation from Enskog’s theory by a correction factor \( F_{\eta} \) again as a function of the molar volume. Furthermore, Tippelkirch et al. \(^{21}\) determined a different temperature dependence of the effective hard-sphere diameter for the liquid phase to be

\[ \sigma_{\text{eff}}^L = 2.81 \, \text{Å} \left( \frac{234 \, \text{K}}{T} \right)^{0.0912}. \]  
The liquid shear viscosity is then given by

\[ \eta^L = \eta_0 \left( \frac{b_L}{v_L} \right) \left( \frac{\chi b_L}{v_L} \right)^{-1} + 0.800 + 0.761 \left( \frac{\chi b_L}{v_L} \right) F_{\eta} \]  
with the superscript \( L \) indicating that \( b \) and \( \eta_0 \) have to be recalculated with the \( \sigma_{\text{eff}} \) of the liquid phase. Inserting again \( \chi \) and \( F_{\eta} \) given by Alder and co-workers \(^{24,25}\) and experi-

FIG. 2. The comparison of data for the self-diffusion coefficient of mercury along the vapor-liquid coexistence obtained from molecular dynamics (□) by using Eq. (2) with prediction (■) based on the modified Enskog theory from Eqs. (21)–(23), and simulation results and predictions by Belashchenko (Ref. 31) (○).
Belanshchenko\textsuperscript{31} performed some simulations for the self-diffusion coefficient by employing discrete values of an effective pair potential derived from structural diffraction data. His results may serve as a comparison for the diffusion coefficient in liquid mercury. Additionally, a similar procedure to that used by Tippelkirch et al.\textsuperscript{21} for the shear viscosity of mercury can be used to calculate the self-diffusion coefficient along the whole VLE saturation line.

The self-diffusion coefficient of a dilute gas is given by\textsuperscript{24}

\begin{equation}
D_0 = \frac{0.425 \nu}{\lambda N_A \sigma_{\text{eff}}^2} \sqrt{\frac{N_A k T M}{\pi}},
\end{equation}

where \(M\) is the molar mass. Again, the Enskog theory relates the self-diffusion coefficient in a dense gas to that of a dilute gas by using the high-density correction\textsuperscript{32}

\begin{equation}
D^L = D_0^L / \chi.
\end{equation}

To describe the self-diffusion coefficient in the liquid phase, the deviation from the Enskog theory can likewise be expressed by a correction factor \(F_D\),

\begin{equation}
D^L = D_0^L F_D / \chi.
\end{equation}

With the temperature-dependent hard-sphere diameters \(\sigma^L\) and \(\sigma_{\text{eff}}^L\) and experimental data\textsuperscript{12,17,20–28} for the molar volumes of the equilibrium phases, Eq. (21) yields the reference self-diffusion coefficients \(D^L_0\) and \(D^V_0\) for the vapor and liquid phases, respectively. By introducing \(F_D\) and \(\chi\) given by Alder and co-workers,\textsuperscript{24,25} the self-diffusion coefficient along the saturation line can be determined from Eqs. (22) and (23).

Figure 2 compares our molecular dynamics simulation results with the calculation of the self-diffusion coefficient as described above, and the simulation results from Belanshchenko.\textsuperscript{31} It illustrates that our simulation results are in good agreement with those given by Belanshchenko. Furthermore, our simulation results for the self-diffusion coefficient reproduce the slope of the saturation line in good accordence and consistency with the description given by the modified Enskog theory, even without applying any long-range corrections.

The fact that our empirical effective potential, which was only determined to give good agreement with experimental liquid phase VLE densities, also yields reasonable results for other completely independent properties is an encouraging outcome. The vapor densities,\textsuperscript{1} the equilibrium pressures,\textsuperscript{1} the pair distribution functions,\textsuperscript{1} and now even the shear viscosities and self-diffusion coefficients can be predicted with a reasonable degree of accuracy over a wide range of state points. It suggests that it is maybe possible to account for nonadditive contributions of multibody effects by combining an accurate two-body \textit{ab initio} potential with an empirically determined multibody contribution via an effective term, if the state dependency of this effective term is adequately chosen.

Due to the good results of our simulations near the critical point, we also performed a power-law analysis to deduce the critical exponent from the shape of the coexistence curve for the shear viscosity and the self-diffusion coefficient. It

\begin{equation}
\rho^L - \rho^V = B \left( \frac{T_C - T}{T_C} \right) ^{\beta}\n\end{equation}

has been shown by Hensel and co-worker\textsuperscript{2–4} that the shape of the coexistence curve of the saturated densities of mercury can be well described by the scaling law

\begin{equation}
\eta^L - \eta^V = \beta \eta \left( \frac{T_C - T}{T_C} \right) ^{\beta_\eta}\n\end{equation}

and the self-diffusion coefficients

\begin{equation}
|D^L - D^V| = B_D \left( \frac{T_C - T}{T_C} \right) ^{\beta_D},
\end{equation}

respectively. We only considered simulation results close to the critical point, i.e., for \(T \approx 1728.15\) or \(\Delta T/T_C \approx 0.013\), and obtained \(\beta_\eta = \beta_D = 0.39\), as shown in Fig. 3. Our value for \(\beta\) is higher than the value of \(\beta = 0.36\) derived by Hensel and co-worker\textsuperscript{2–4,12} from the coexisting densities. However, the experimental data used by Hensel and co-worker in their analysis covered a much wider temperature range of \(T = 1073.15–1751.15\) K. As shown in Fig. 3, if the analysis is repeated using saturation densities reported by Götzlaff\textsuperscript{12} for the same temperature range (i.e., \(T \approx 1728.15\) K), a value of \(\beta = 0.39\) is obtained, which is identical to our simulation results.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig3}
\caption{Scaling law analysis (---) of the shear viscosities (\(\eta\)) and the self-diffusion coefficients (\(\beta\)) close to the critical point obtained from molecular dynamics by using Eq. (2), and of the coexisting densities obtained from experiment (Ref. 12) (•).}
\end{figure}

\section{IV. CONCLUSIONS}

In this work an accurate two-body \textit{ab initio} potential by Schwerdtfeger et al.\textsuperscript{11} in combination with an empirically
determined multibody contribution, adjusted to liquid densities of the vapor-liquid equilibria only, was used to predict the shear viscosities and the self-diffusion coefficients of mercury along the saturation line. The results were compared with experimental data and simulation results available and calculations based on an empirical modification of the Enskog theory that involves experimental data for the VLE. Increasing deviations between simulation and experiment indicate that not only a temperature-dependent but also a density-dependent multibody contribution is necessary to reliably predict the viscosity of liquid mercury in metal state points with high densities. However, the reasonably good results for the self-diffusion coefficient and the shear viscosities at moderate densities suggest that it is worthwhile to extend efforts on incorporating the effect of the multibody interactions in \textit{ab initio} pair potentials via state-dependent correction terms.

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